

# Neutrino Oscillation Search from the MINOS Experiment

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# Outline

- Neutrino Oscillation Physics
- The MINOS Experiment
- MuMI Flux Measurement
- MINOS  $\theta_{13}$  Measurement

I will focus on my personal work in this talk.

# 3-Flavor Mixing

Weak state

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

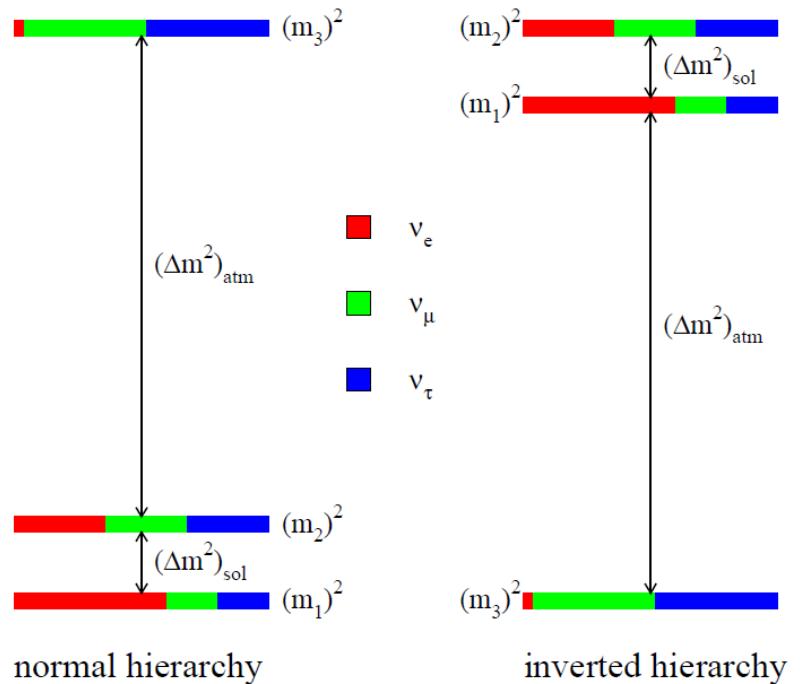
$$m_2^2 > m_1^2$$

$$m_2^2 - m_1^2 \ll |m_3^2 - m_{1,2}^2|$$

$\Delta m_{31}^2 > 0$  Normal Mass Hierarchy

$\Delta m_{31}^2 < 0$  Inverted Mass Hierarchy

Mass state



Pontecorvo-Maki-Nakagawa-Sakata (PMNS) matrix relates the two bases, it can be expressed in 3 mixing angles, 1 CP phase and 2 Majorana phases:

$$\tan^2 \theta_{12} \equiv \frac{|U_{e2}|^2}{|U_{e1}|^2}; \quad \tan^2 \theta_{23} \equiv \frac{|U_{\mu 3}|^2}{|U_{\tau 3}|^2}; \quad U_{e3} \equiv \sin \theta_{13} e^{-i\delta}$$

# PMNS Matrix Measurements

The neutrino mixing (PMNS) matrix can be factorized into 4 experimental regimes:

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta_{23} & \sin \theta_{23} \\ 0 & -\sin \theta_{23} & \cos \theta_{23} \end{pmatrix} \begin{pmatrix} \cos \theta_{13} & 0 & e^{-i\delta_{CP}} \sin \theta_{13} \\ 0 & 1 & 0 \\ -e^{-i\delta_{CP}} \sin \theta_{13} & 0 & \cos \theta_{13} \end{pmatrix} \begin{pmatrix} \cos \theta_{12} & \sin \theta_{12} & 0 \\ -\sin \theta_{12} & \cos \theta_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} e^{i\alpha_1/2} & 0 & 0 \\ 0 & e^{i\alpha_2/2} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

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Solar  $\nu$  (SNO)  
KamLand  
Future reactors

$$\Delta m_{21}^2 \sim 7.9 \times 10^{-5} \text{ eV}^2$$
$$\theta_{12} \sim 34^\circ$$

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Atmospheric ν  
K2K, SuperK  
MINOS  
Off-axis

$$|\Delta m^2_{32}| \sim 2.4 \times 10^{-3} \text{ eV}^2$$

$$\theta_{23} \sim 45^\circ$$

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CHOOZ/Palo Verde  
K2K, MINOS  
Future reactors  
Off-axis NOvA, T2K

$\theta_{13} < 11^\circ$  at 90% C.L.

Solar ν (SNO)  
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<b>Atmospheric</b> Atmospheric ν K2K, SuperK MINOS Off-axis	<b>Cross-mixing</b> CHOOZ/Palo Verde K2K, MINOS Future reactors Off-axis NOvA, T2K	<b>Solar</b> Solar ν (SNO) KamLand Future reactors	<b>Majorana</b> Neutrinoless double beta decay
$ \Delta m^2_{32}  \sim 2.4 \times 10^{-3} \text{ eV}^2$ $\theta_{23} \sim 45^\circ$	$\theta_{13} < 11^\circ$ at 90% C.L.	$\Delta m^2_{21} \sim 7.9 \times 10^{-5} \text{ eV}^2$ $\theta_{12} \sim 34^\circ$	

# 2-Flavor Neutrino Oscillation

$\theta$  is the mixing angle

$$P_{osc} = \sin^2 2\theta$$

$$\Delta m^2 = m_1^2 - m_2^2 (\text{eV}^2)$$

$$\frac{1.27 \Delta m^2 L}{E}$$

L is the distance that neutrino travels (km)

E is neutrino energy (GeV)

Different oscillation experiments are generally sensitive to only **one mass scale** ( $\Delta m^2 L / E = O(1)$ ), 2-flavor approximation can be used.

If  $\Delta m^2 L / E \ll 1$ ,  $\sin^2(1.27 \Delta m^2 L / E) \approx 0$ ; if  $\Delta m^2 L / E \gg 1$ ,  $\sin^2(1.27 \Delta m^2 L / E) \approx 1/2 \rightarrow$  average over E and L

# Overview of the MINOS Experiment

- **MINOS (Main Injector Neutrino Oscillation Search)**

- a long baseline neutrino oscillation experiment
- sensitive to the atmospheric mass scale ( $L/E \sim 235[\text{km}/\text{GeV}]$ )

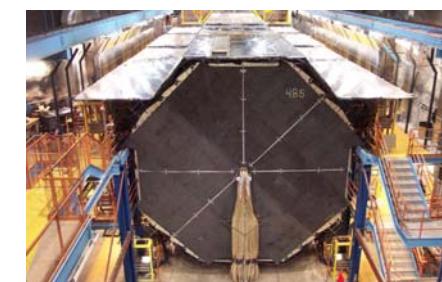
Two functional identical detectors.

■ Far Detector:

- Mass: 5.4 kt
- Distance : 735km

■ Near Detector:

- Mass: 1kt
- Distance : 1km



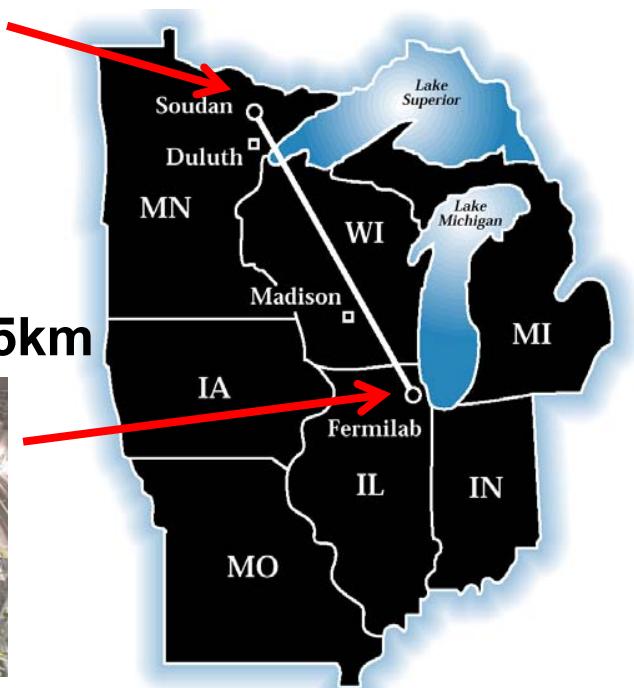
Far Detector 735km



Near Detector

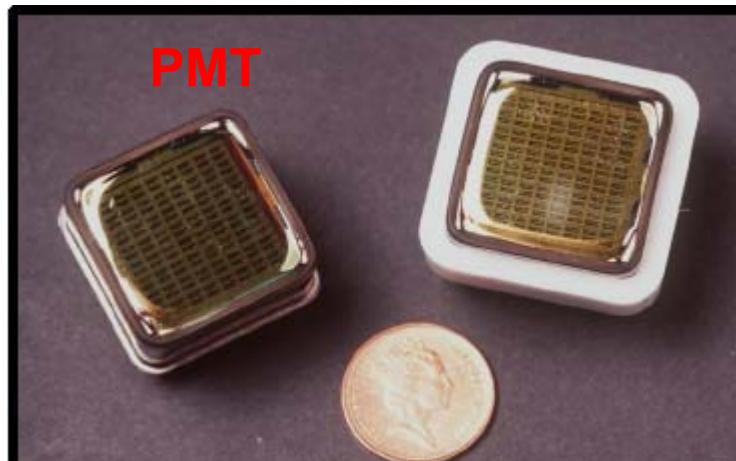
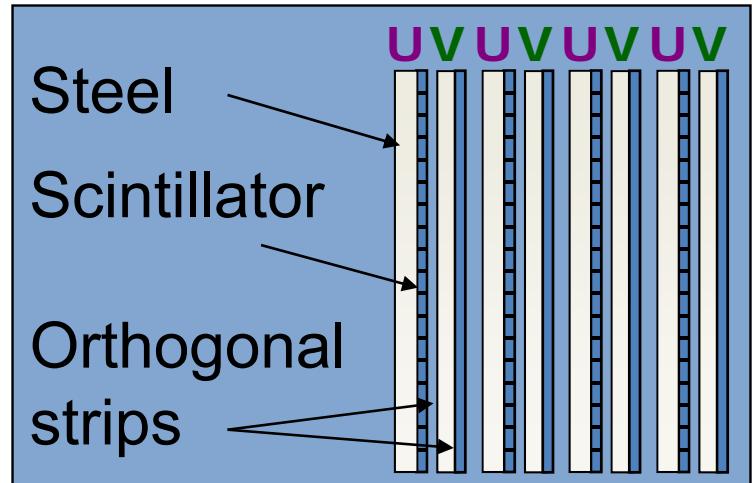
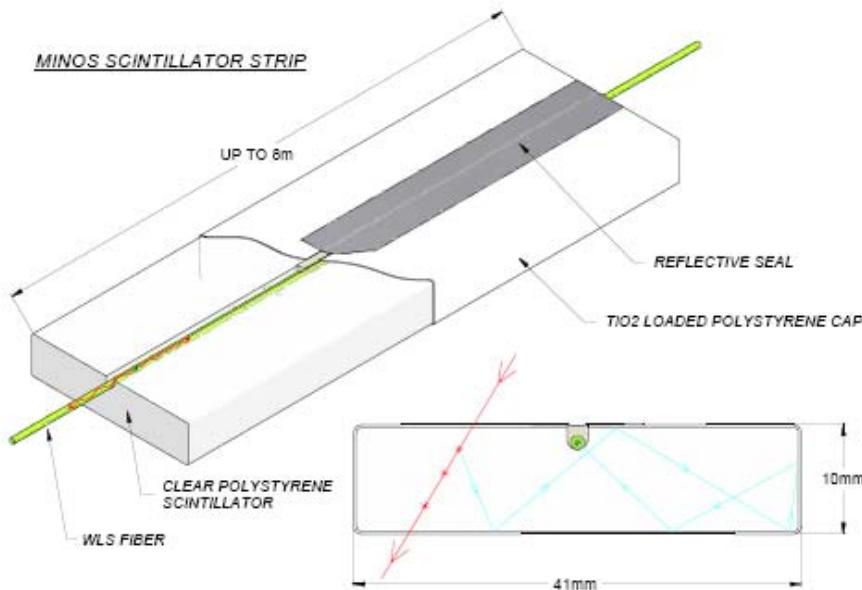
$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

$\nu_e$  appearance       $\nu_\mu$  disappearance



# MINOS Detector Technology

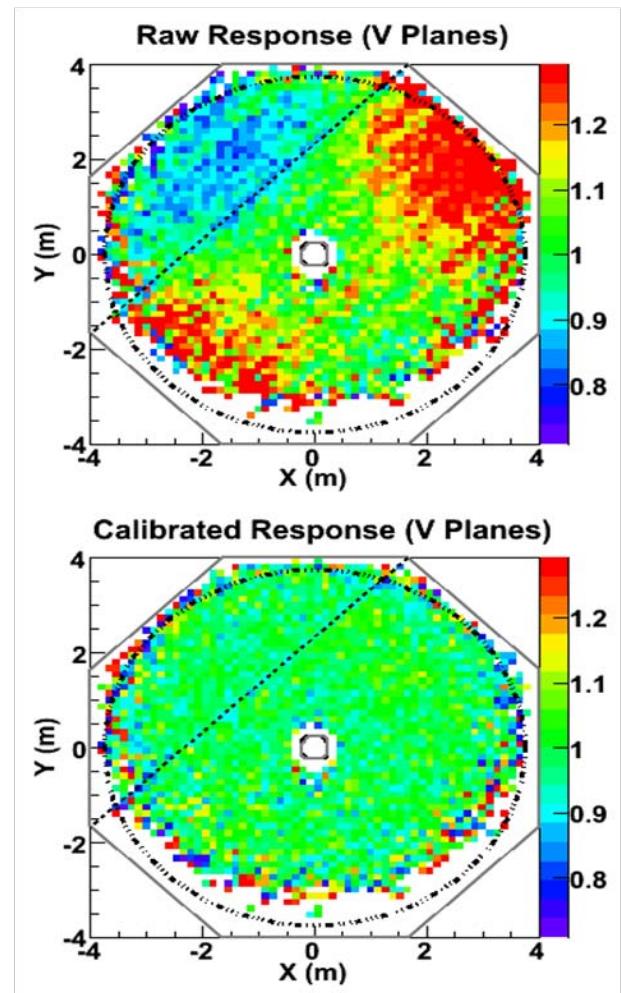
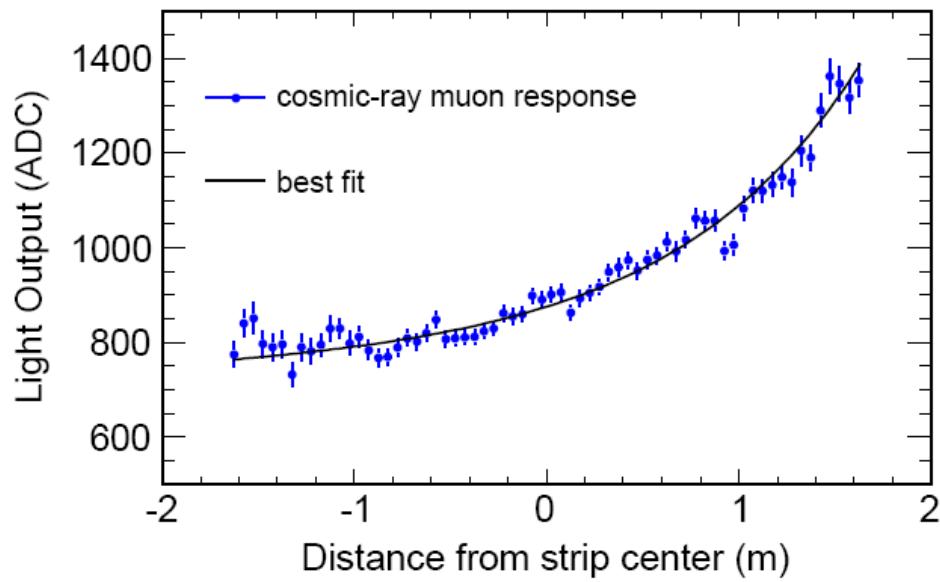
## Magnetized Iron/scintillator tracking calorimeter



- Steel: 2.54cm thick
- Scintillator: 1cm thick, 4.1cm wide strips
- Alternate planes rotated by  $\pm 90^\circ$  (U,V)
- Wavelength shifting fibers (WLS)
- Multi-anode Hamamatsu PMTs

# Detector Calibration

- Measure & remove spatial and temporal variations (channel difference , attenuation , detectors)
- Attenuation Calibration
  - mapper data sample
  - cosmic-ray muon sample



# Detector Calibration

MINOS Calibration detector (CalDet):

- Exposed to 0.2-10GeV p, e,  $\mu$ ,  $\pi$  at CERN

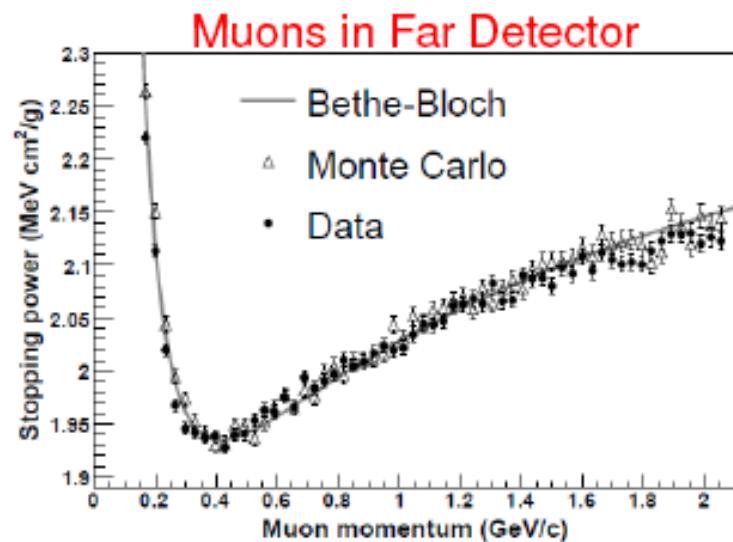
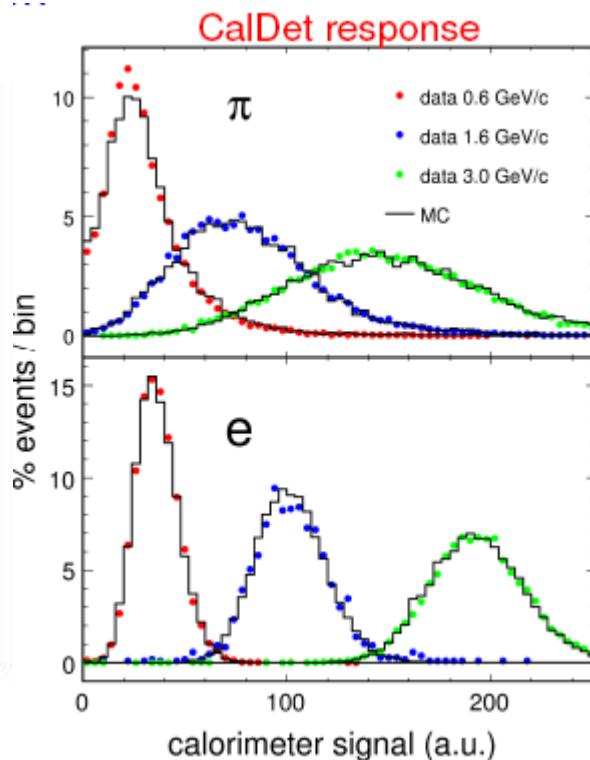
Energy resolution:

Hadrons:  $56\%/\sqrt{E}$       Electrons:  $21\%/\sqrt{E}$

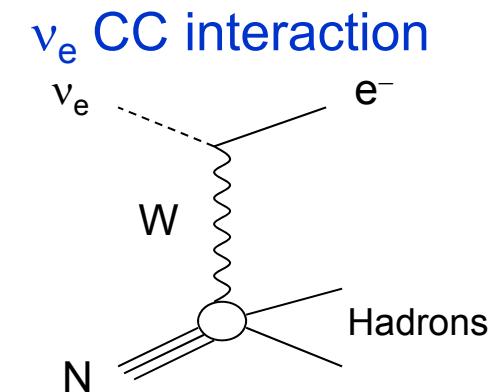
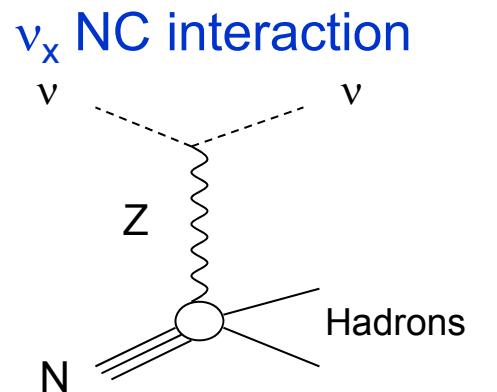
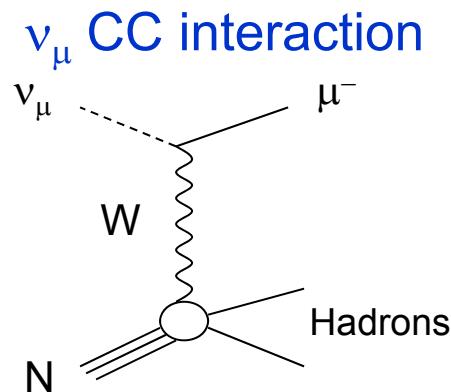
Energy Scale Uncertainty: ND-FD relative: 2%    Absolute: 6%



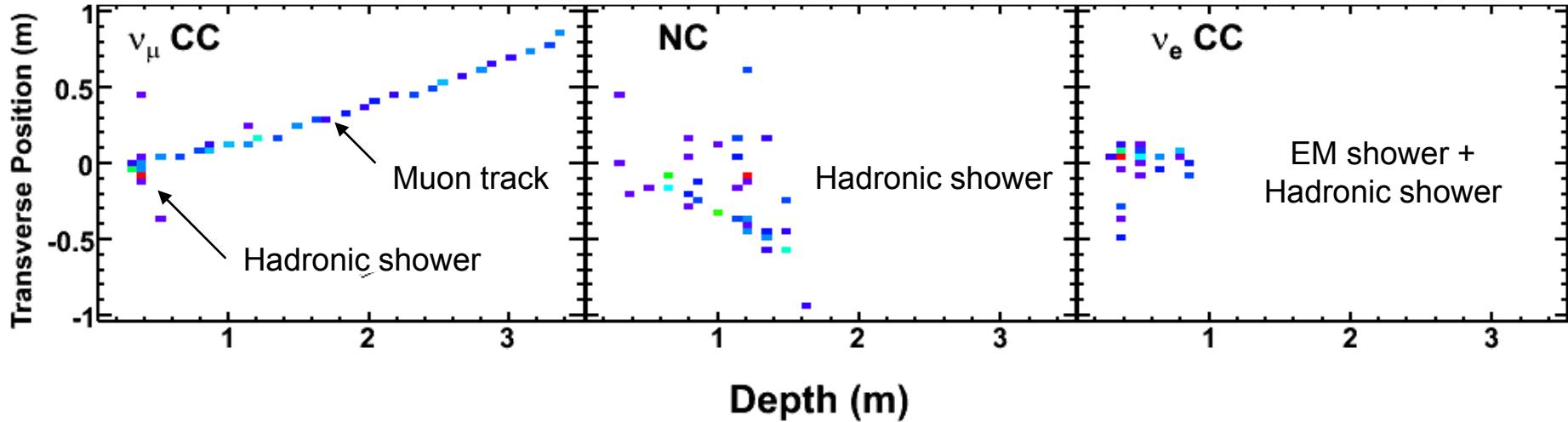
CalDet



# Event Reconstruction



Monte Carlo



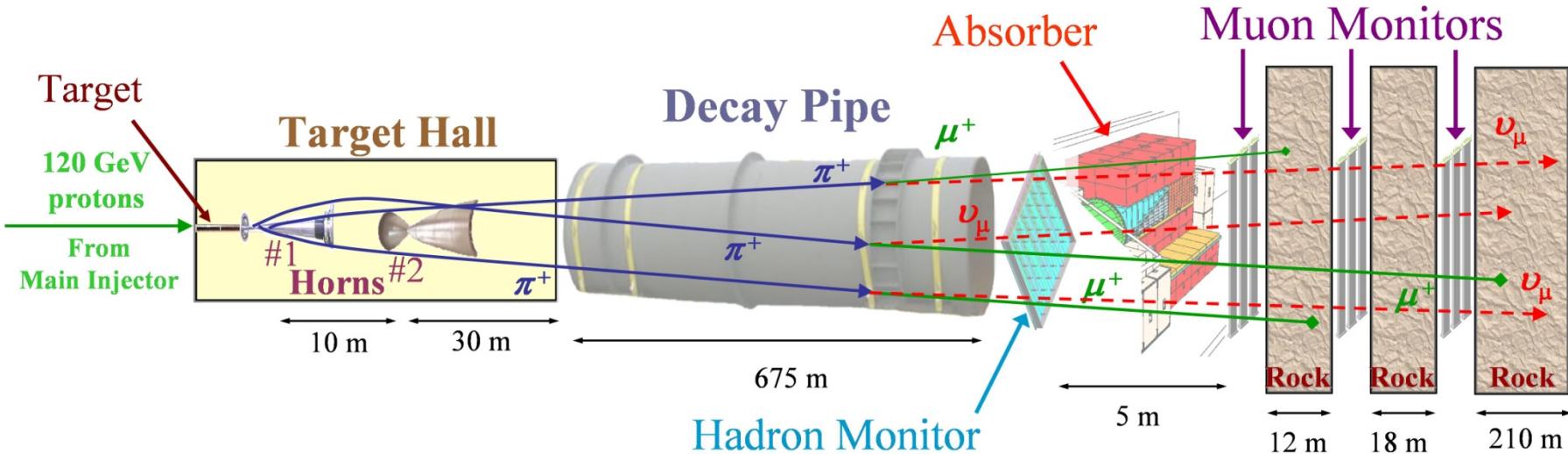
clean channel for  $\nu_\mu$  disappearance

background to  $\nu_\mu$  CC and  $\nu_e$  CC

search for  $\nu_e$  appearance

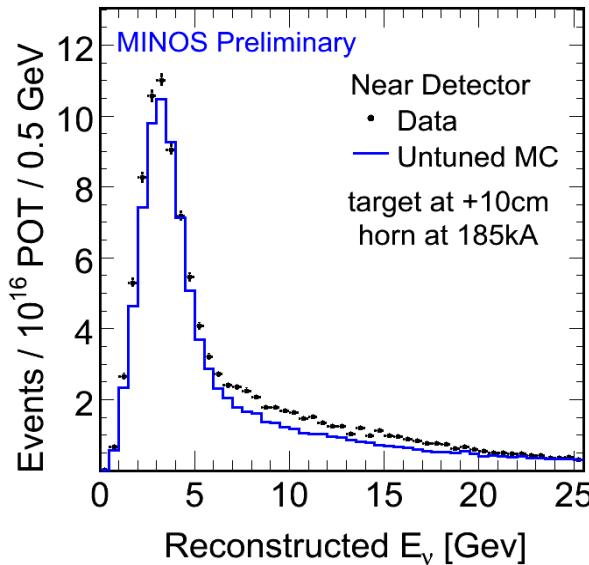
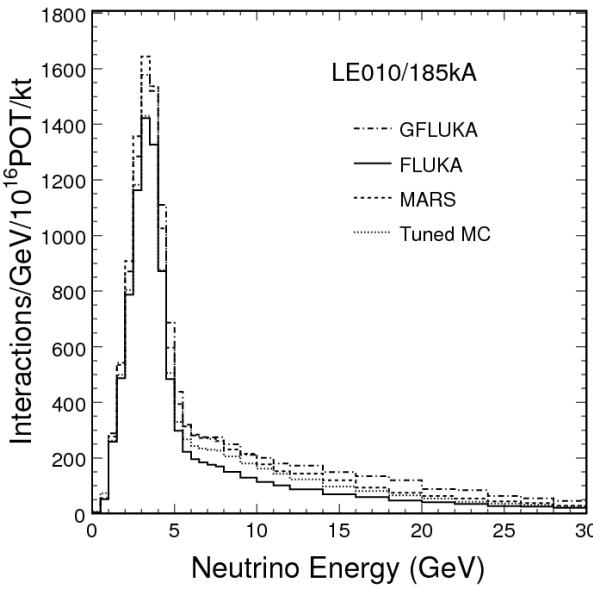
# NuMI Flux Measurement

# Neutrinos at Main Injector (NuMI)



- 120 GeV protons from Fermilab MI
- 1m segments of graphite target
- 2 focusing horns
- Mesons decay in the decay pipe to give a beam of neutrinos
- Various neutrino energy spectra by varying the relative positions of target and horns
- In the Low Energy configuration: 92.9%  $\nu_\mu$ , 5.8%  $\bar{\nu}_\mu$ , 1.3%  $\nu_e + \bar{\nu}_e$

# NuMI Flux Simulation



- Determining neutrino flux is quite hard:
  - Use FLUKA05 + GEANT3 MC simulation
  - Various cascade models indicate hardron production uncertainty 10-30%.
  - The neutrino + nucleon X-section uncertainty below 10GeV .
  - Beam-line simulation uncertainty.
  - Large uncertainty associated with MIPP measurement for the NuMI target .

# Low- $\nu$ Relative Flux Extrapolation

- D. Naple and S.R. Mishra introduced a low- $\nu$  relative flux extrapolation method.
- It relies on the independence of the neutrino(anti-neutrino) differential cross section  $d\sigma/d\nu$  with energy in the limit  $\nu \rightarrow 0$

$$\frac{d^2\sigma^{\nu(\bar{\nu})}}{dxdy} = \frac{{G_F}^2 ME}{\pi} \left[ \left( 1 - y - \frac{Mxy}{2E} \right) F_2^{\nu(\bar{\nu})} + \frac{y^2}{2} 2xF_1^{\nu(\bar{\nu})} \pm y \left( 1 - \frac{y}{2} \right) xF_3^{\nu(\bar{\nu})} \right]$$

Using  $\nu = E \times y$ , and integrating the differential Xsec given above over x (from 0 to 1)

$$\boxed{\frac{d\sigma}{d\nu} = A \left( 1 + \frac{B}{A} \frac{\nu}{E} - \frac{C}{A} \frac{\nu^2}{2E^2} \right)}$$

$$A = \frac{G_F^2 M}{\pi} \int F_2(x) dx$$

$$B = -\frac{G_F^2 M}{\pi} \int (F_2(x) \mp xF_3(x)) dx$$

$$C = B - \frac{G_F^2 M}{\pi} \int F_2(x) \left( \frac{1+2Mx/\nu}{1+R(x)} - \frac{Mx}{\nu} - 1 \right) dx$$

As  $\nu \rightarrow 0$ , the Xsection becomes independent of neutrino energy.

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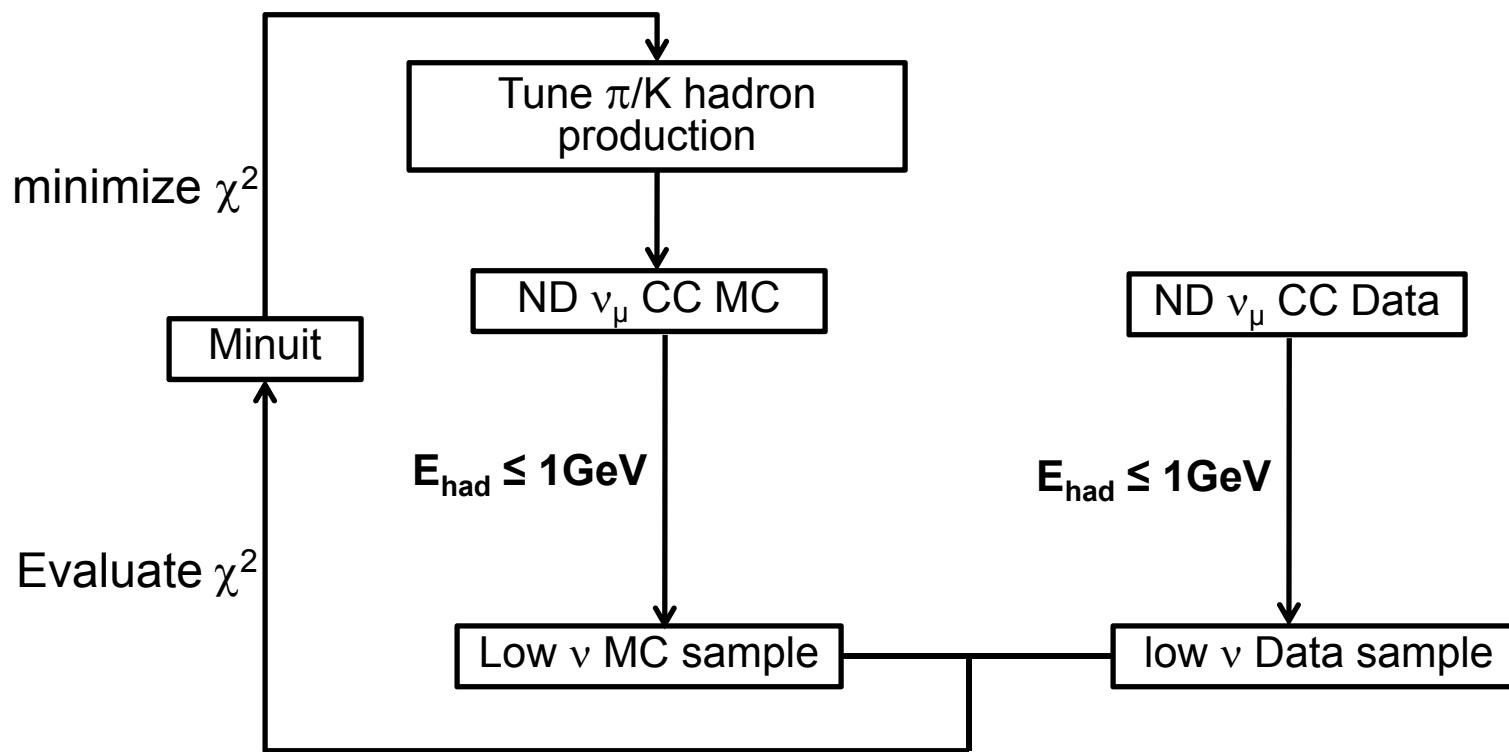
Times flux on both sides and integrating the shower energy from 0 to 1

$$N(E)_{(\nu \leq 1 \text{ GeV})} = \Phi(E) \cdot A \int_0^1 \left( 1 + \frac{B}{A} \frac{\nu}{E} - \frac{C}{A} \frac{\nu^2}{2E^2} \right) d\nu$$

the number of events in a given energy bin with hadronic energy less than 1GeV is proportional to the neutrino flux.

# Empirical Parameterization (EP) Method

- In order to predict the neutrino flux in the Far Detector, we need to retune the  $\pi/K$  hadron production by using the low- $\nu$  flux sample.



# Hadron Production Parameterization

Parameterize the  $\pi/K$  hadron production yield as a function of  $x_R$  ( $x_F$ ) and  $p_T$ .

$$E \times \frac{d^3\sigma}{dp^3} = A(1 - x_R)^\alpha (1 + Bx_R)x_R^{-\beta} \times (1 + a'(x_R)p_T + b'(x_R)p_T^2)e^{-a'(x_R)p_T}$$

where  $a'(x_R) = a / x_R^\gamma$  and  $b'(x_R) = a^2 / 2x_R^\delta$  arxiv: hep-ph/0101163

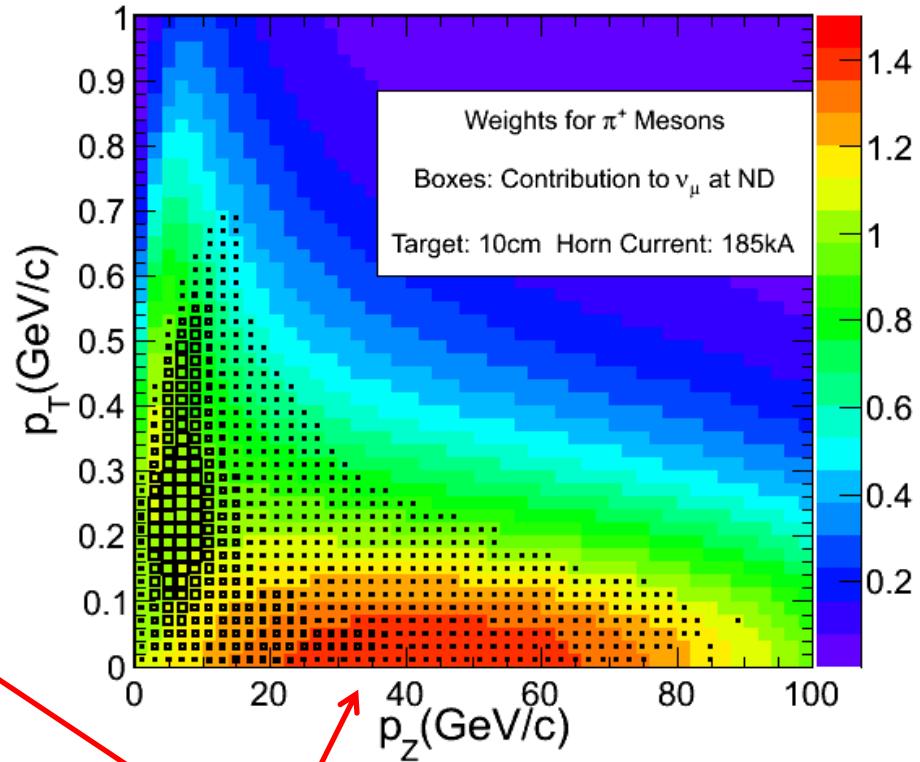
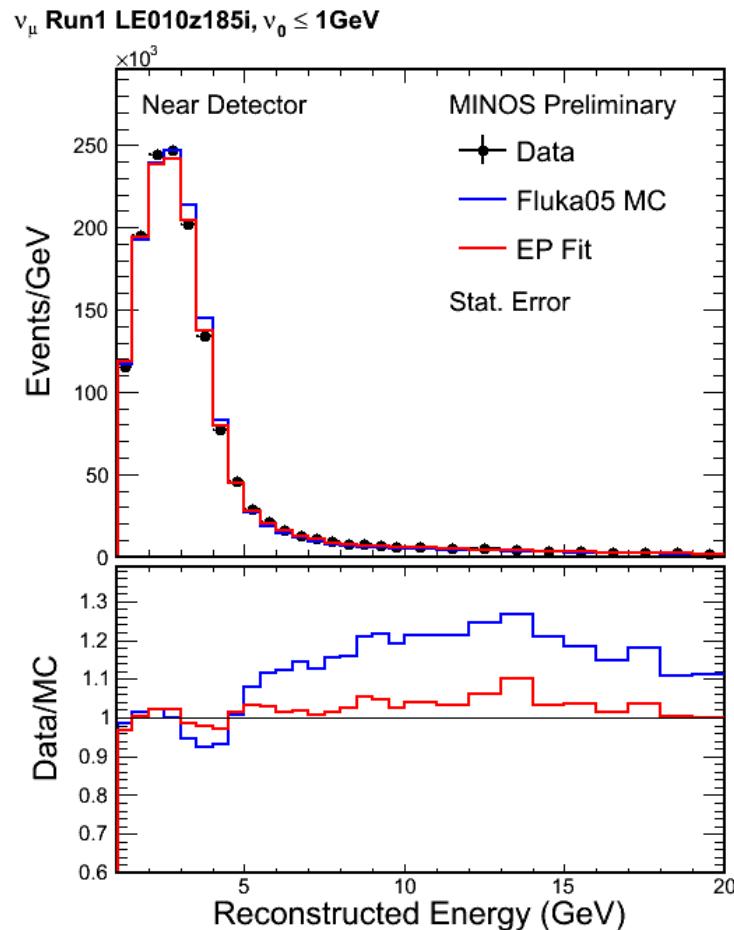
BMPT Function

14 parameters are used: 7 for pion and 7 for Kaon.

- By varying these parameters, we can tune the neutrino flux shape.

$$Weight = \frac{BMPT(x_R, p_T, A', B', a', \dots)}{BMPT(x_R, p_T, A, B, a, \dots)}$$

# Fit to Low- $\nu$ ND Data

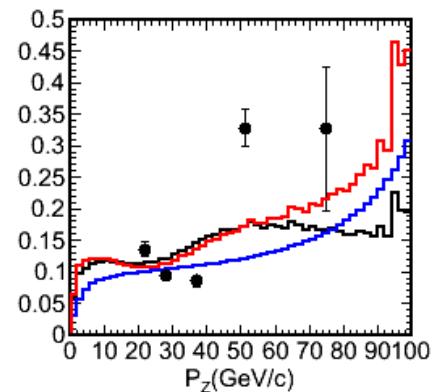


The EP retuned flux can fit the ND data within 10% level.

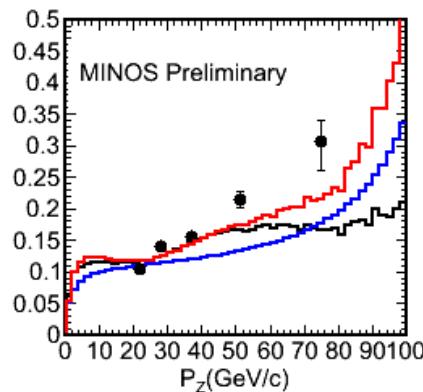
# Hadron Ratios

$K^+/\pi^+$

$K^+/\pi^+$  ratio, pt[0, 0.2]GeV

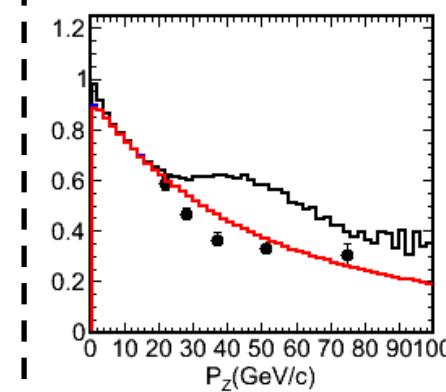


$K^+/\pi^+$  ratio, pt[0.2, 0.4]GeV

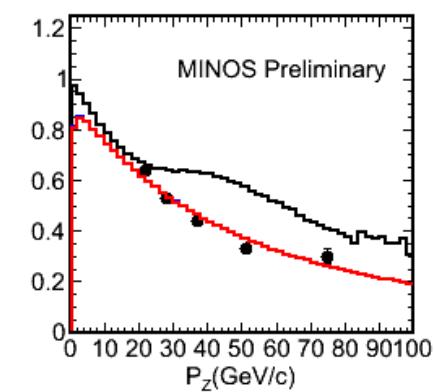


$\pi^-/\pi^+$

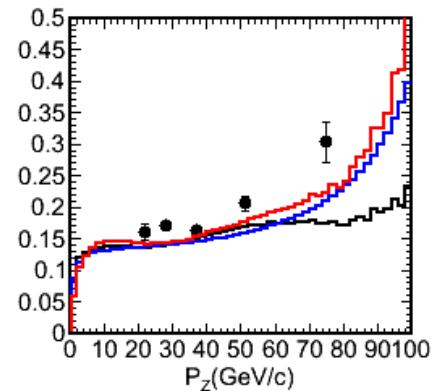
$\pi^-/\pi^+$  ratio, pt[0, 0.2]GeV



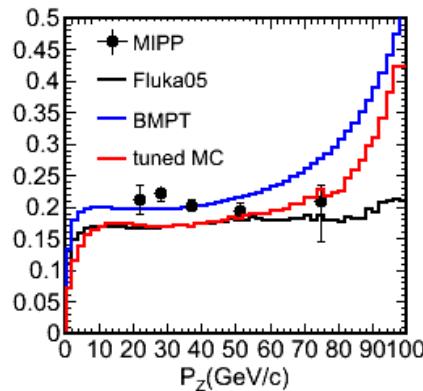
$\pi^-/\pi^+$  ratio, pt[0.2, 0.4]GeV



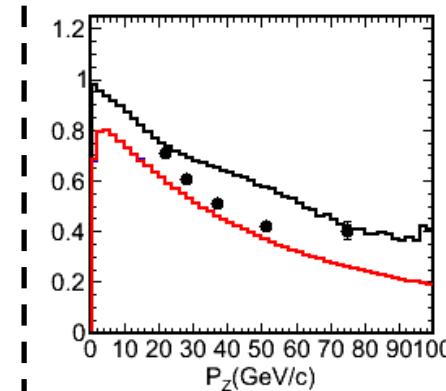
$K^+/\pi^+$  ratio, pt[0.4, 0.6]GeV



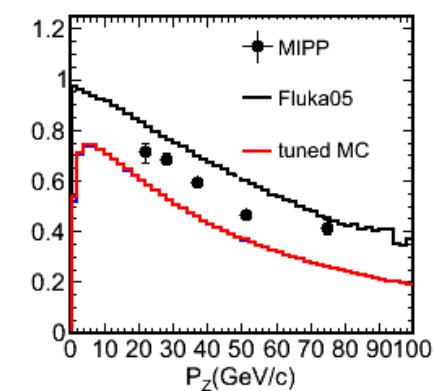
$K^+/\pi^+$  ratio, pt[0.6, 1.0]GeV



$\pi^-/\pi^+$  ratio, pt[0.4, 0.6]GeV



$\pi^-/\pi^+$  ratio, pt[0.6, 1.0]GeV



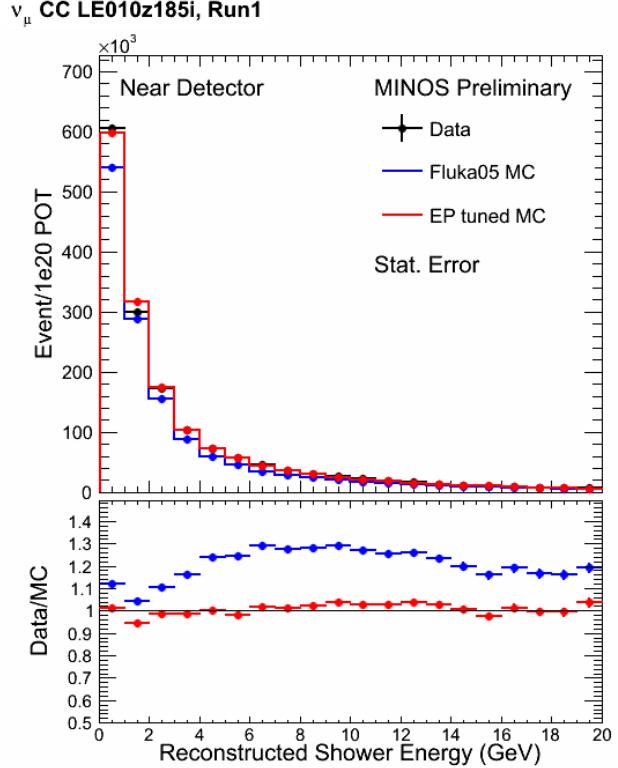
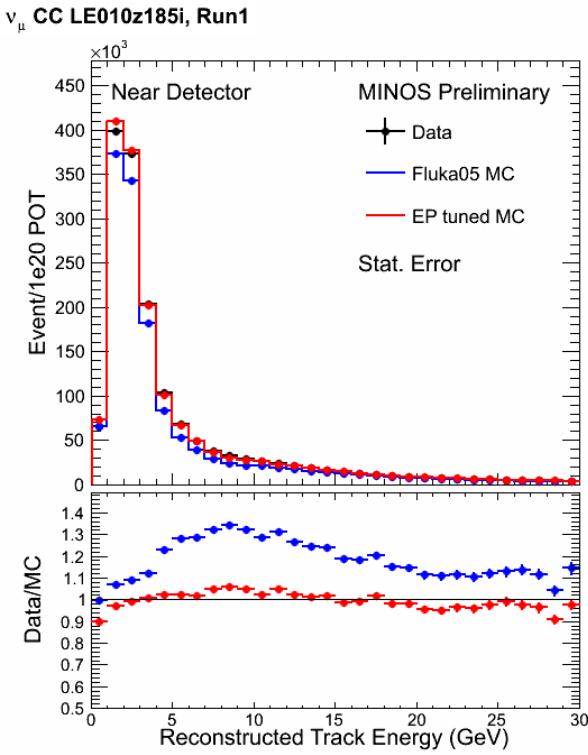
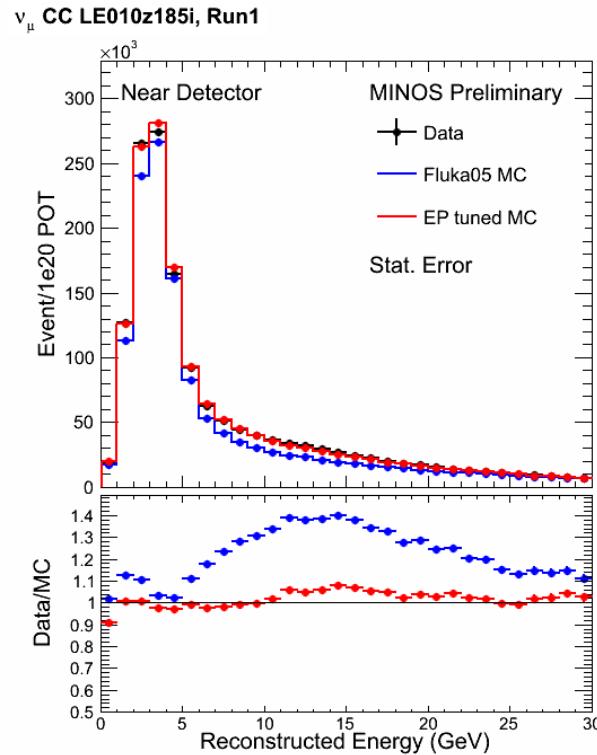
Fluka05

BMPT

Tuned MC

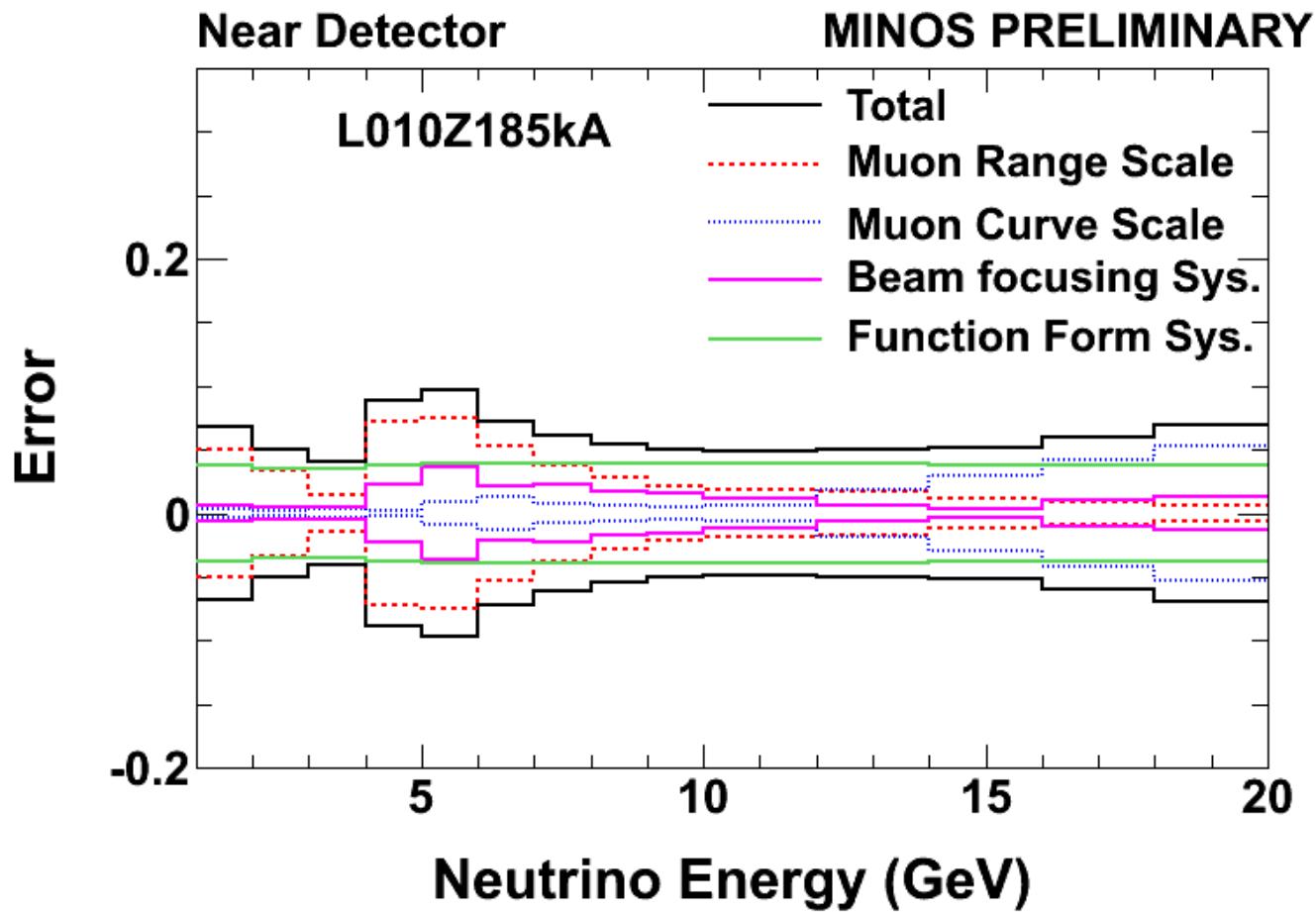
MIPP

# Full Sample Data/MC Comparison



With the ND low- $\nu$  data constraint, EP retuned MC has a better agreement with ND data.

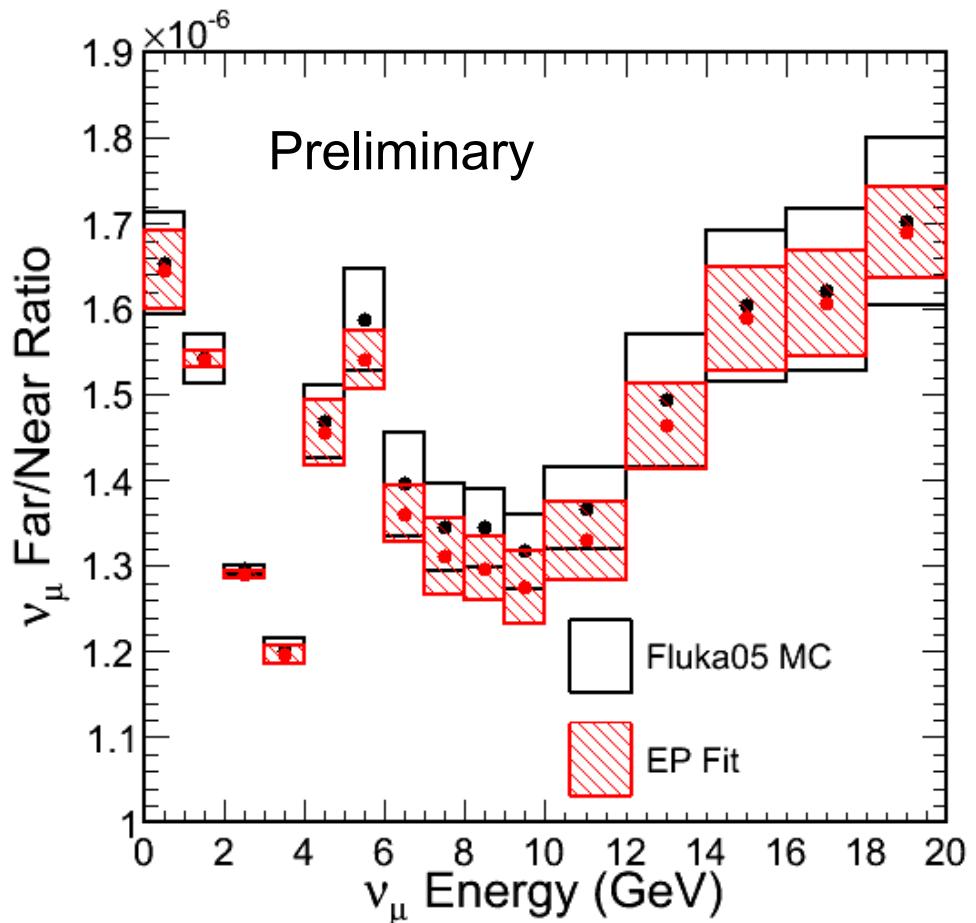
# Systematic Uncertainty



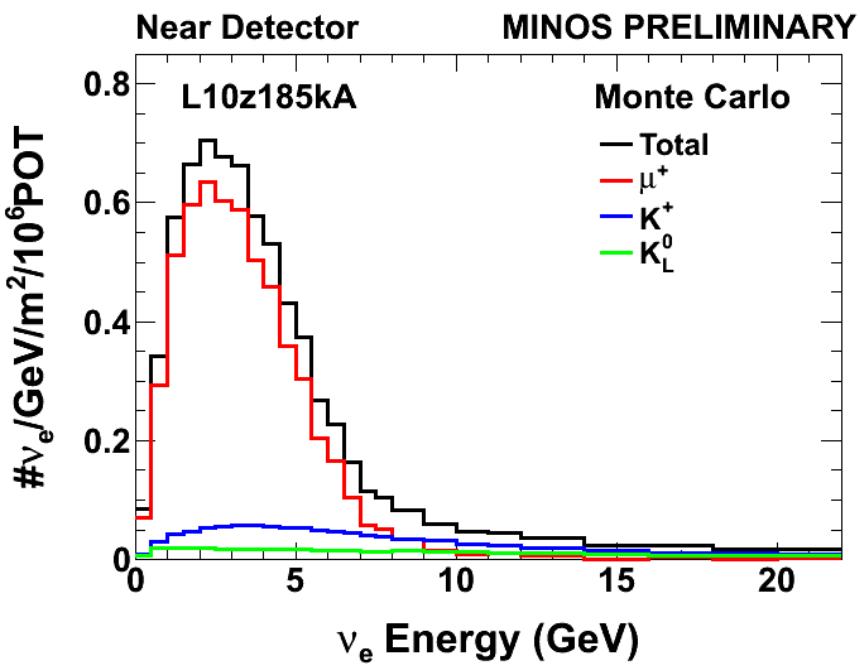
# F/N Ratio Comparison

EP fit MC is able to reduce the systematic uncertainties on the F/N ratio.

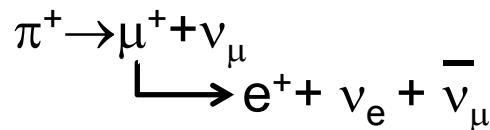
The dominant errors come from muon energy scale and horn focusing.



# Beam $\nu_e$ Determination



Source	0-8 GeV	8-20 GeV
$\mu^+$	85%	21%
$K^+$	11%	52%
$K_L^0$	4%	27%



$\nu_e$  from 1-8 GeV (region of interest by the  $\nu_e$  oscillation analysis) is dominated by  $\mu^+$  decay and it is well constrained by the  $\pi^+$  fit.

$\nu_e$  flux uncertainty is less than 10%.

# Summary of EP Method

- Merit
  - Accurately predict  $\nu_\mu$  relative flux by using the ND low- $\nu$  data (independent of  $\nu$  xsec).
  - Reduce the systematic uncertainty on F/N ratio.
  - $\nu_e$  flux can be constrained by the  $\pi/K$  fit.
  - Data/MC agreement improvement.
- Disadvantage
  - Level of agreement between the fit and low- $\nu$  data
  - Sensitive to the muon energy scale

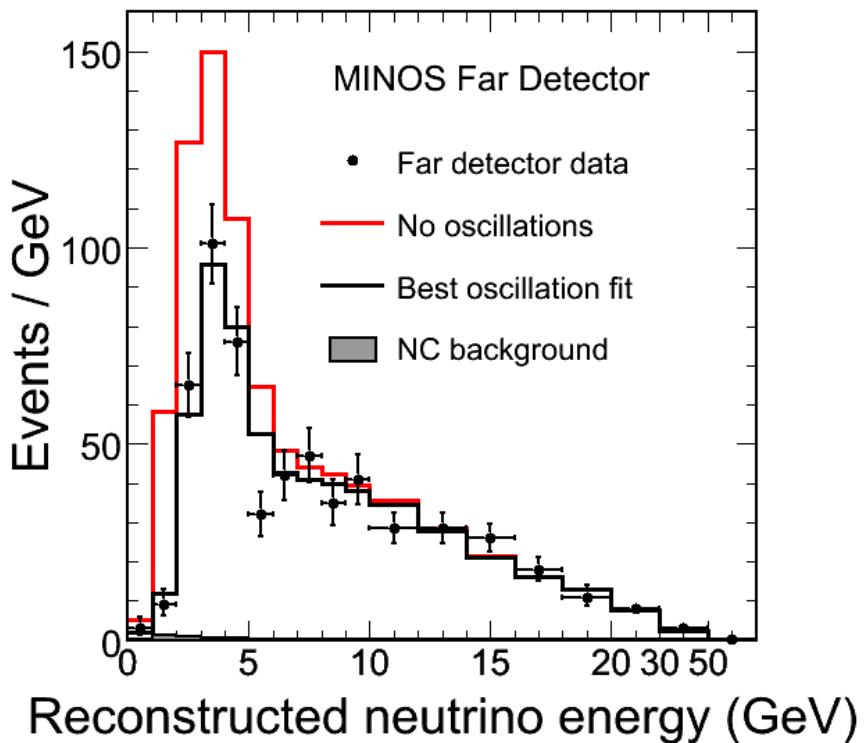
# MINOS $\theta_{13}$ Measurement

# $\nu_\mu$ CC Disappearance Results

$$P(\nu_\mu \rightarrow \nu_\mu) = 1 - \sin^2 2\theta_{23} \sin^2 \left( \frac{1.27 \Delta m_{32}^2 L}{E} \right)$$

$|\Delta m_{32}^2| = 2.43 \pm 0.13 \times 10^{-3} \text{ eV}^2$  (68% C.L.)

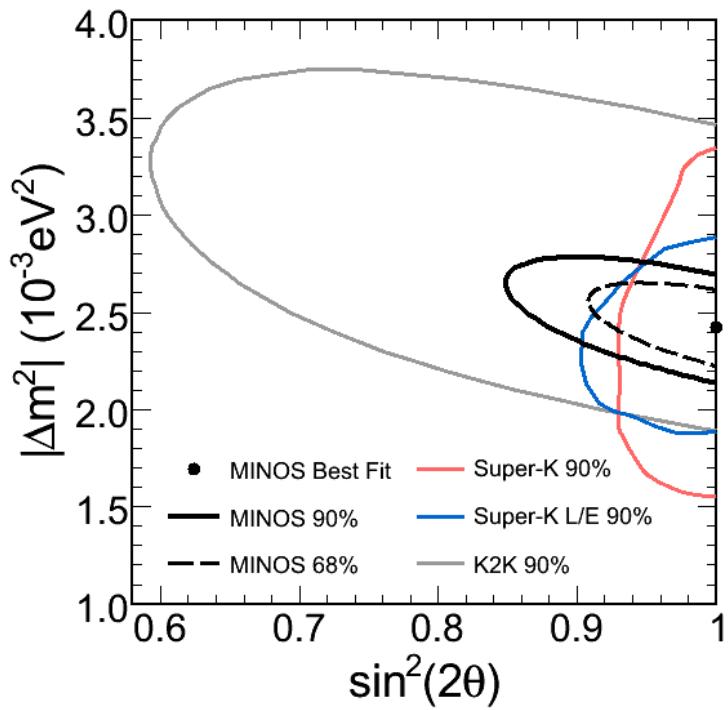
$\sin^2(2\theta_{23}) > 0.90$  (90% C.L.)



Expected:  $1065 \pm 60$  events

Observed: 848 events

Most precise measurement of  $|\Delta m_{32}^2|$



Phys. Rev. Lett. 101: 131802 (2008)

# $\nu_e$ Appearance

$$P(\nu_\mu \rightarrow \nu_e) \approx \sin^2 \theta_{23} \boxed{\sin^2 2\theta_{13}} \sin^2 \left( 1.27 \Delta m_{31}^2 L / E \right)$$

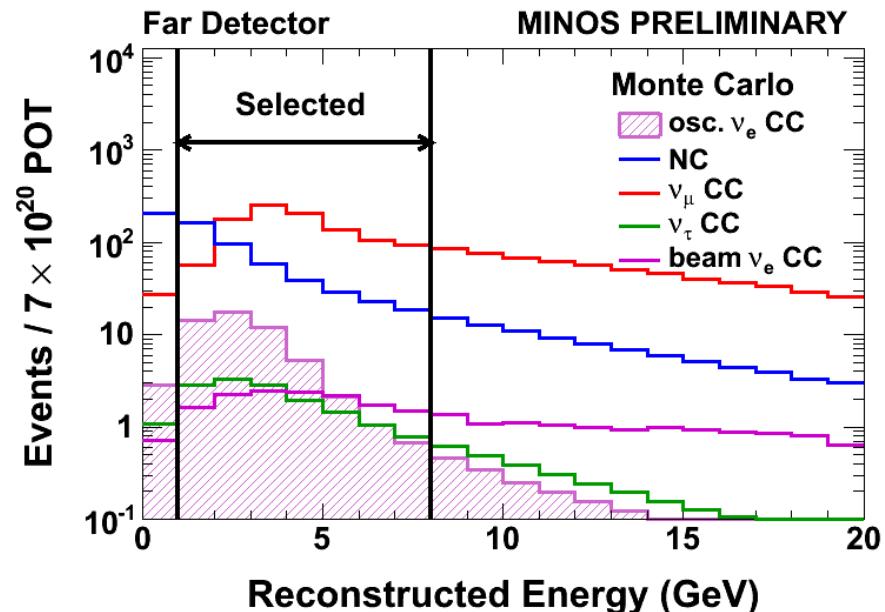
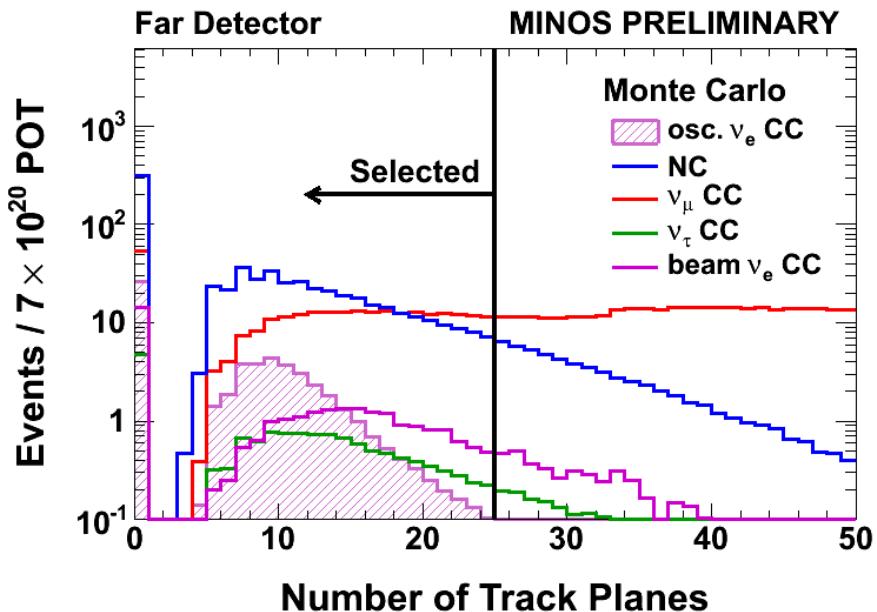
Leading order term

- **Analysis Approach**
  - Determine the selection criteria for  $\nu_e$  candidate events
  - Use ND data to decompose background components
  - Extrapolate ND background components to FD taking into account  $\nu_\mu \rightarrow \nu_\tau$  oscillations
  - Measuring/constraining  $\theta_{13}$  by looking for excess of  $\nu_e$ -like events in the FD

# Challenge of MINOS $\nu_e$ Selection

- Difficulties for the  $\nu_e$  analysis
  - $\nu_\mu \rightarrow \nu_e$  oscillation is the sub-dominant oscillation mode in MINOS.
    - Only  $\sim 3\%$  FD events are  $\nu_e$  CC events assuming  $\sin^2(2\theta_{13}) = 0.15$
  - Granularity of the MINOS Detectors
    - Steel thickness = 1.4 radiation length
    - Strip width = 1.2 Moliere radius
  - Various background components
    - NC Hadronic shower events: NC  $\pi^0$
    - High  $y_{bj}$  CC events
    - Intrinsic beam  $\nu_e$  components

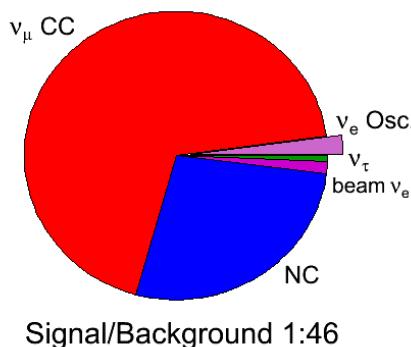
# $\nu_e$ Pre-selection Cuts



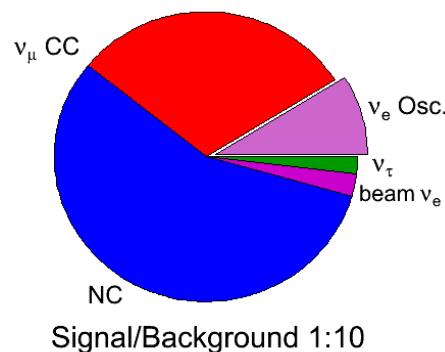
Assuming signal at CHOOZ limit

- Preselection requirements:
  - Track length < 25 planes.
  - Track like length < 16 planes.
  - Reconstructed energy 1-8 GeV.
  - At least one shower and 4 contiguous planes with > 0.5 M energy units.

Fiducial Cut

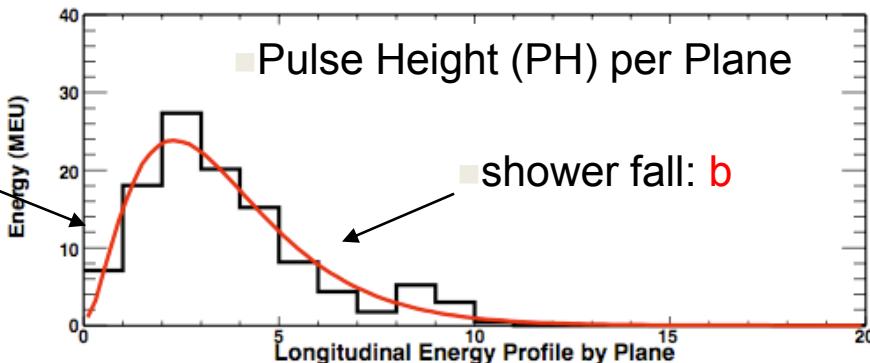


Preselection Cut MC



# Longitudinal Shower Profile

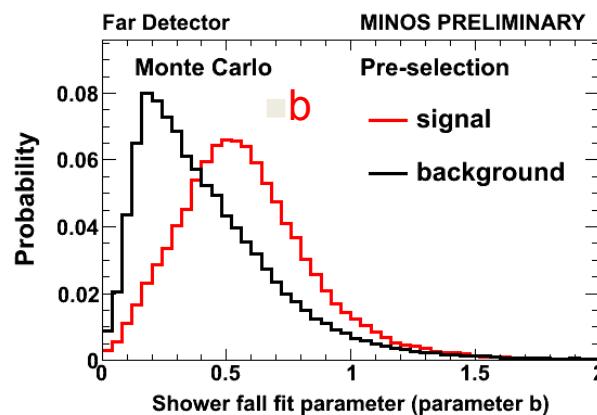
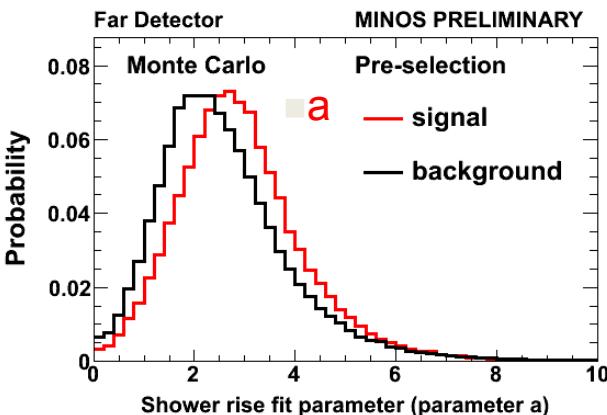
■ shower rise: **a**



■ The average longitudinal profile of the energy deposition in an EM shower is reasonably well described by a gamma distribution:

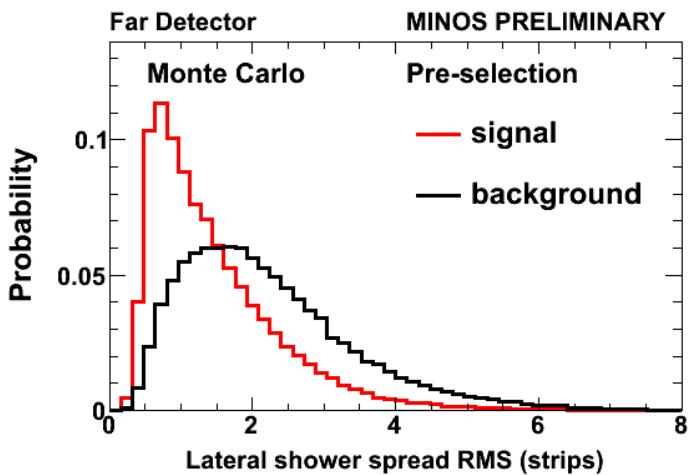
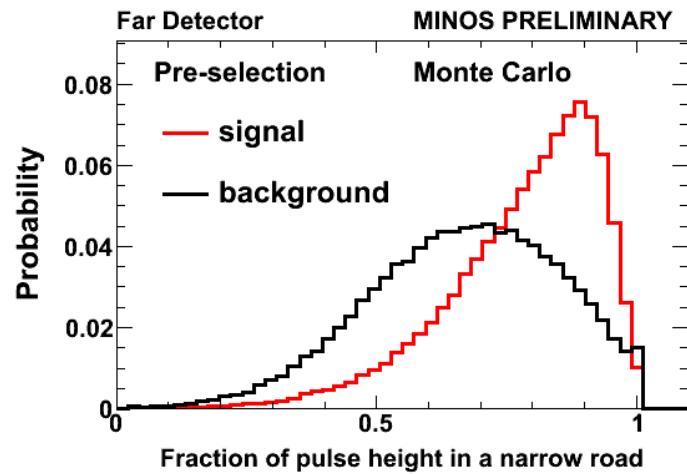
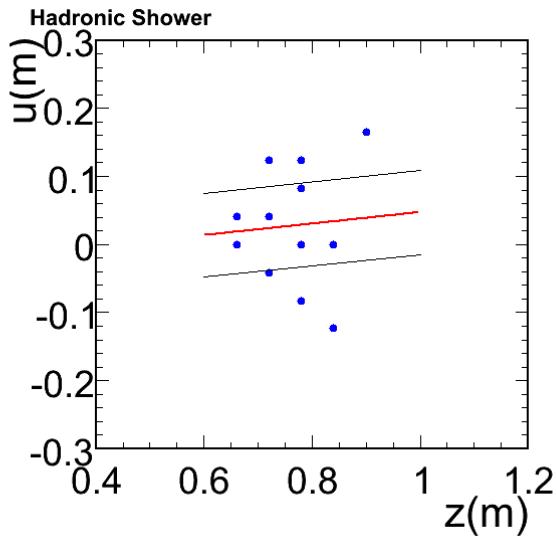
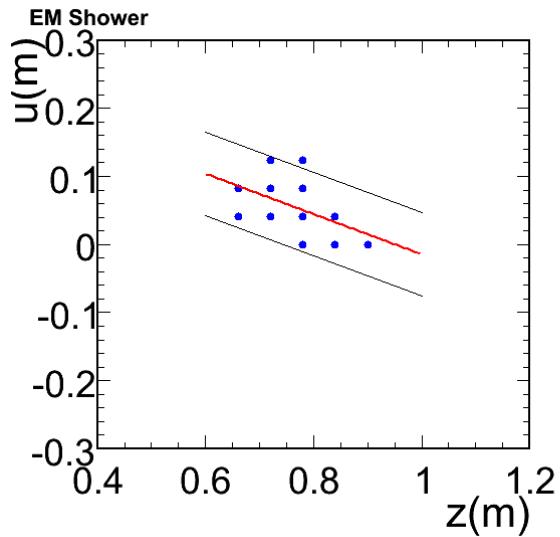
$$\frac{dE}{dt} = E_0 b \frac{(bt)^{a-1} e^{-bt}}{\Gamma(a)}$$

$$t = x/X_0 \text{ where } X_0 \text{ is the radiation length}$$



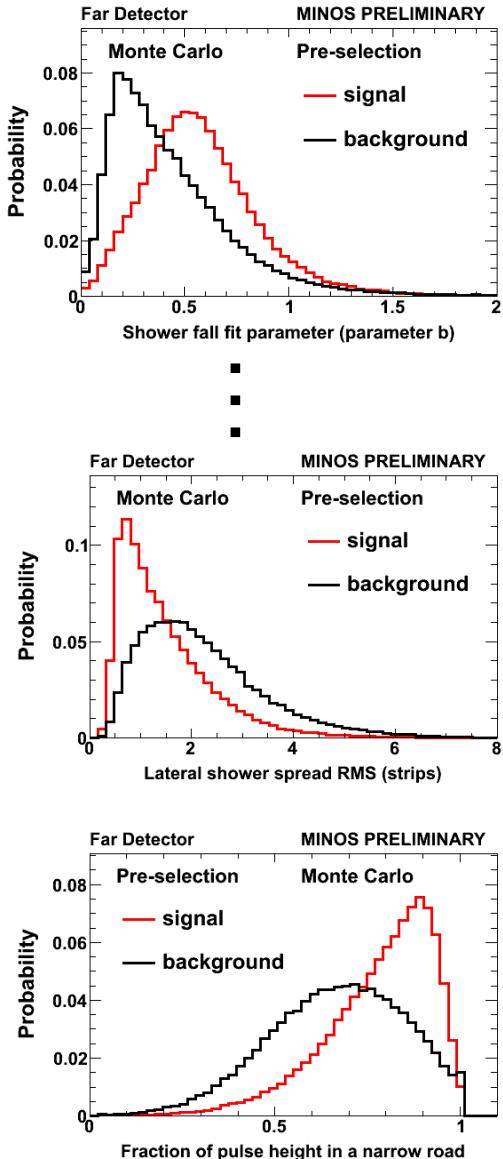
■ Other useful variables:  
 ■ - fraction of energy deposited  
 ■ - within 2,4,6 planes  
 ■ - longitudinal energy projection

# Transverse Shower Profile

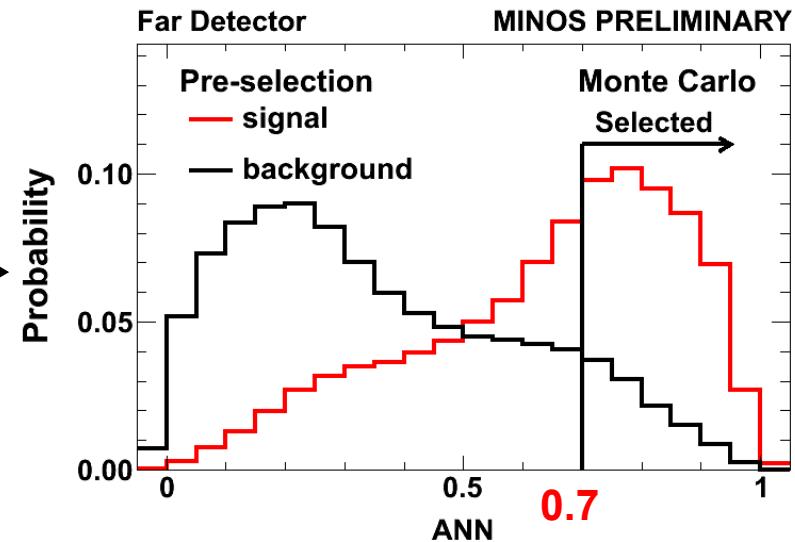
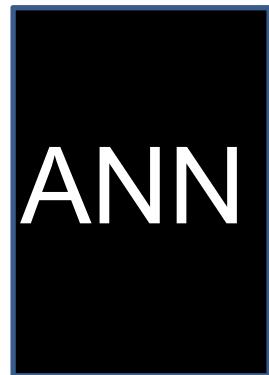


- EM showers are more compact than hadronic showers
- Other useful transverse variables
  - lateral shower spread (RMS)
  - 90% containment radius

# Artificial Neural Network (ANN)

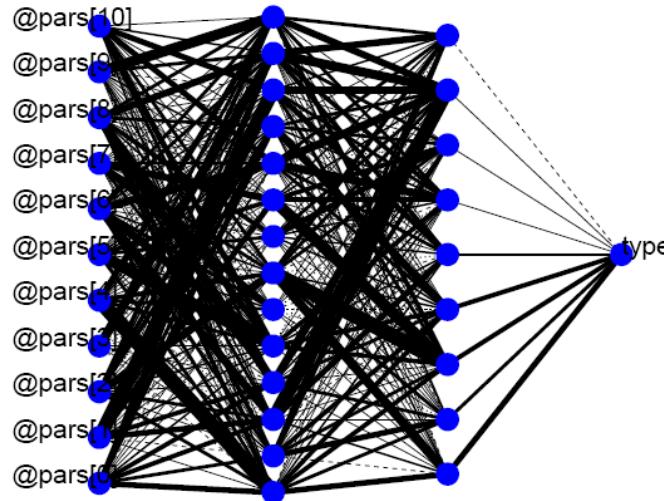
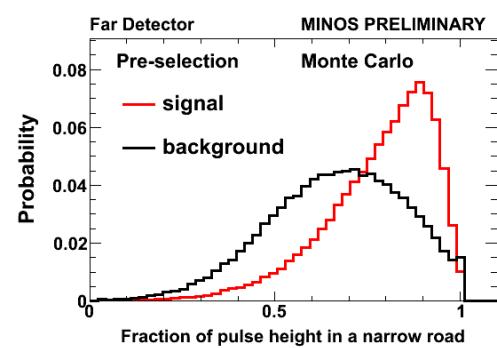
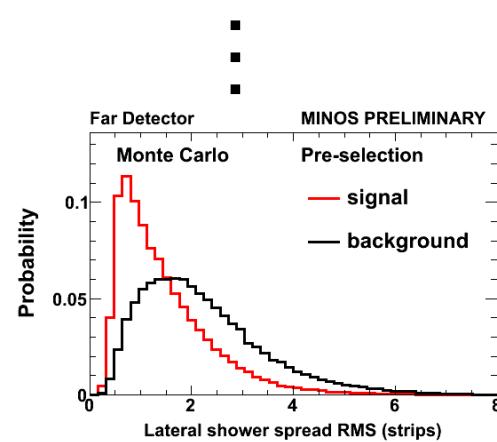
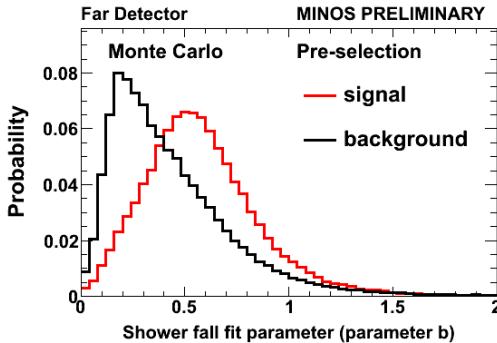


11 discriminating variables derived from the longitudinal and transverse profile of the energy deposition.



Build an neural net (ANN11) to enhance the signal/background separation and take into account the correlations between input variables.

# ANN11 Retuning

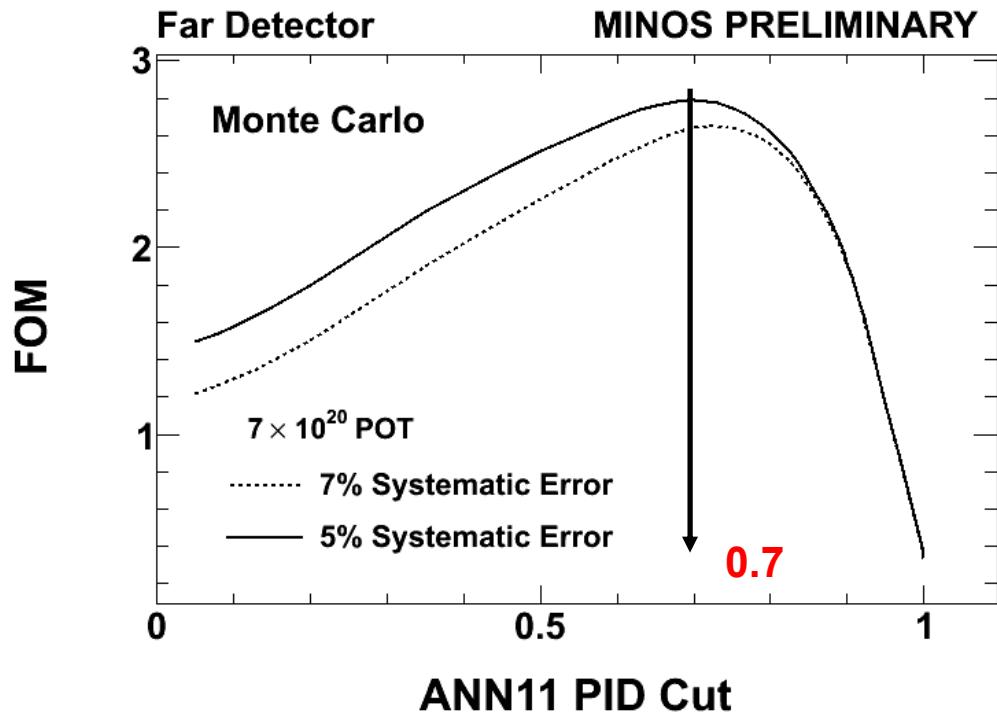
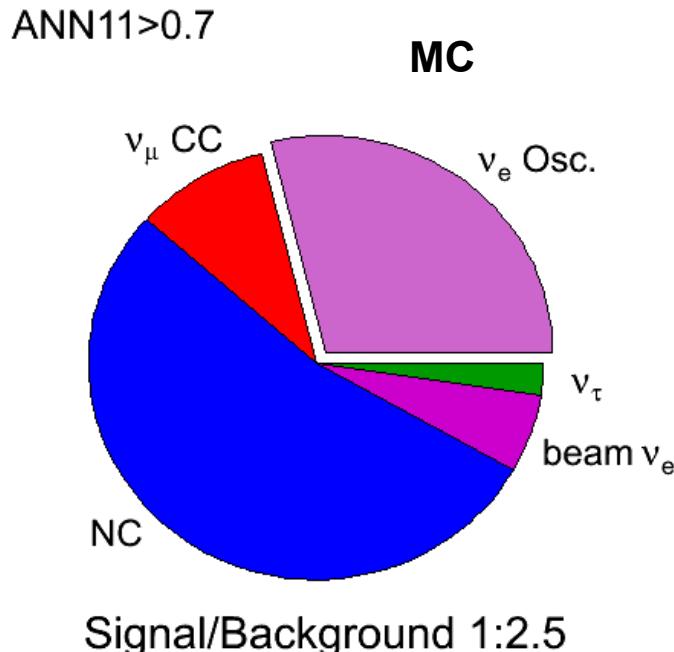


- The architecture of neural net are optimized with more hidden nodes (11:14:9:1)
- The size of training sample are increased by a factor of ten.
- All the input variables are normalized before processing.

# Cut Value Determination

$$FOM = \frac{N_{sig}}{\sqrt{N_{bg} + (\sigma_{sys}^{bg})^2 N_{bg}^2}}$$

$$\sigma_{sys}^{bg} = (5/7)\%$$

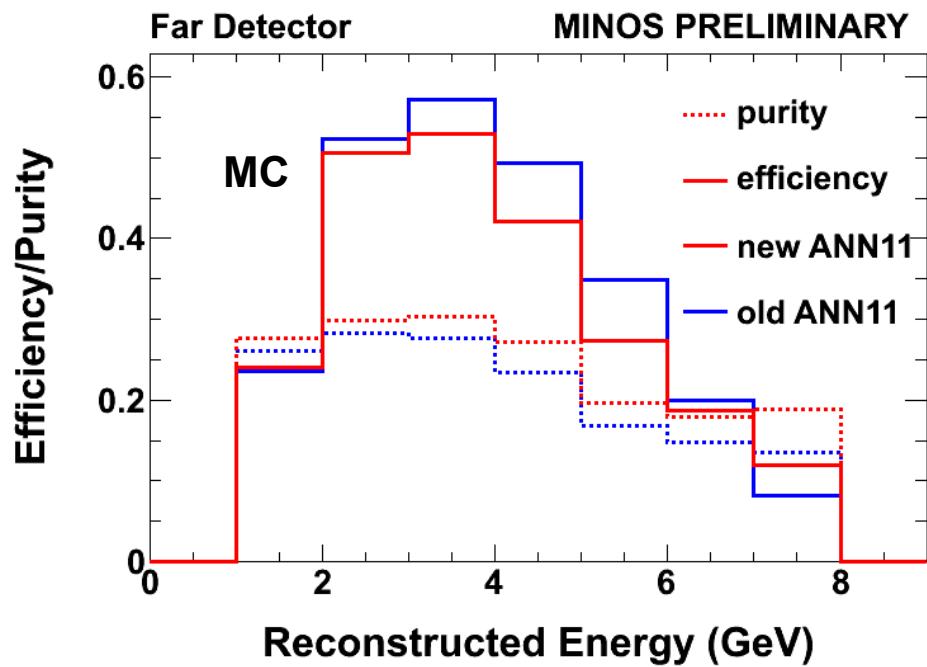
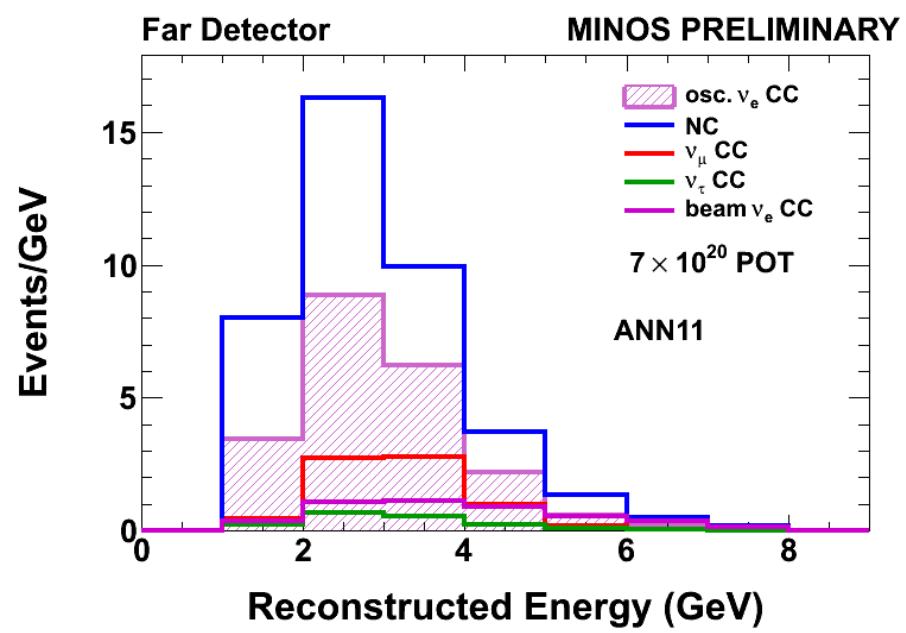


- The cut value is determined by maximizing sensitivity to observe signal events.

$\sin^2(2\theta_{13})=0.15$  (CHOOZ limit),  
 $|\Delta m^2_{31}|=2.43 \text{e-3 eV}^2$ ,  $\sin^2(2\theta_{23})=1$ .  
 POT = 7E20 (4-year exposure).

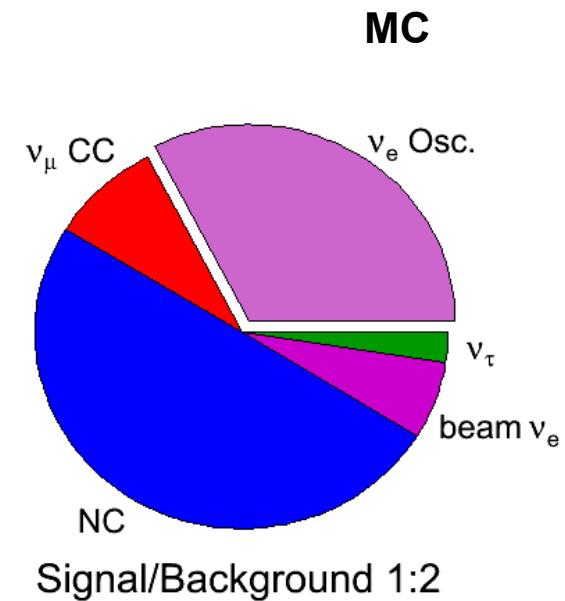
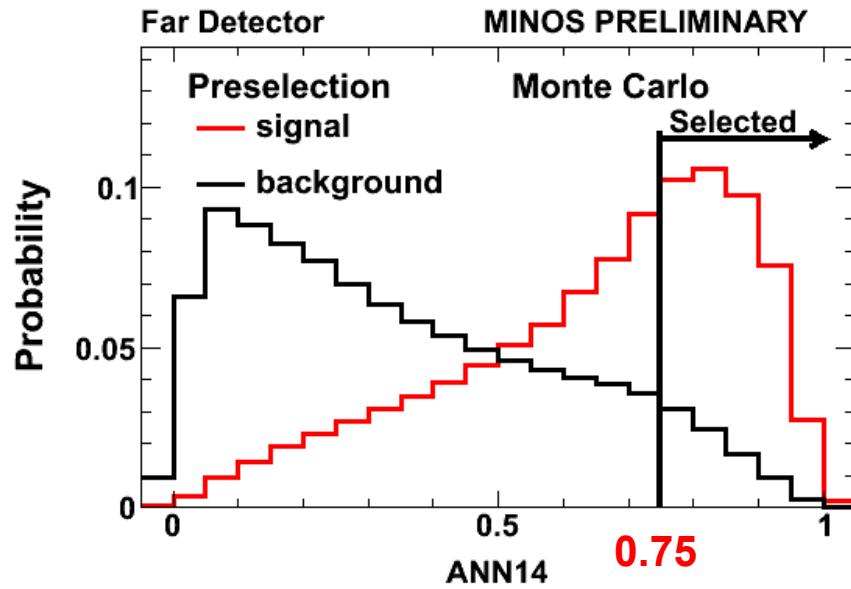
# Signal Efficiency and Background Rejection

PID	signal	background	FOM (MC only)
ANN11(new)	37.6%	97.9%	$2.77\sigma$
ANN11(old)	39.8%	97.6%	$2.66\sigma$

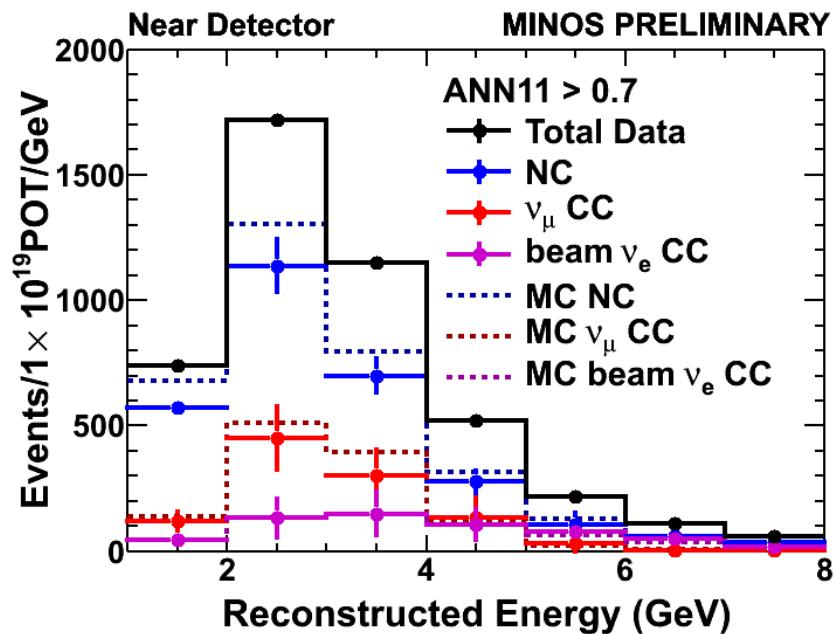
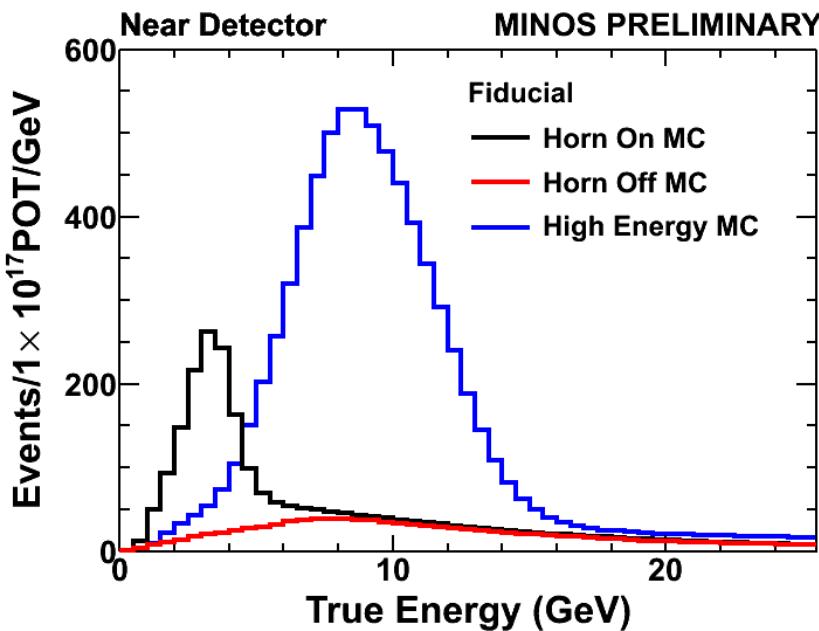


# Further Improvement Attempt

- 20 more new variables are added into a large neural net
- Systematically removing each variable to evaluate the weight of the variable.
- 14 most powerful variables are selected for the another PID: ANN14.
- A better signal/background discrimination power.
- Relatively large systematic uncertainties (7%).
- The FOM of ANN14 is effectively the same as ANN11 PID.



# Decomposition & Extrapolation



Monte Carlo can't be relied on to determine the background components due to large uncertainties in the hadronization model. We can use ND data with different beam configurations to do the ND background decomposition

FD prediction for component  $\alpha$  in energy bin i

$$F_i^{predicted,\alpha} = N_i^\alpha \times \left( \frac{f_i^\alpha}{n_i^\alpha} \right)$$

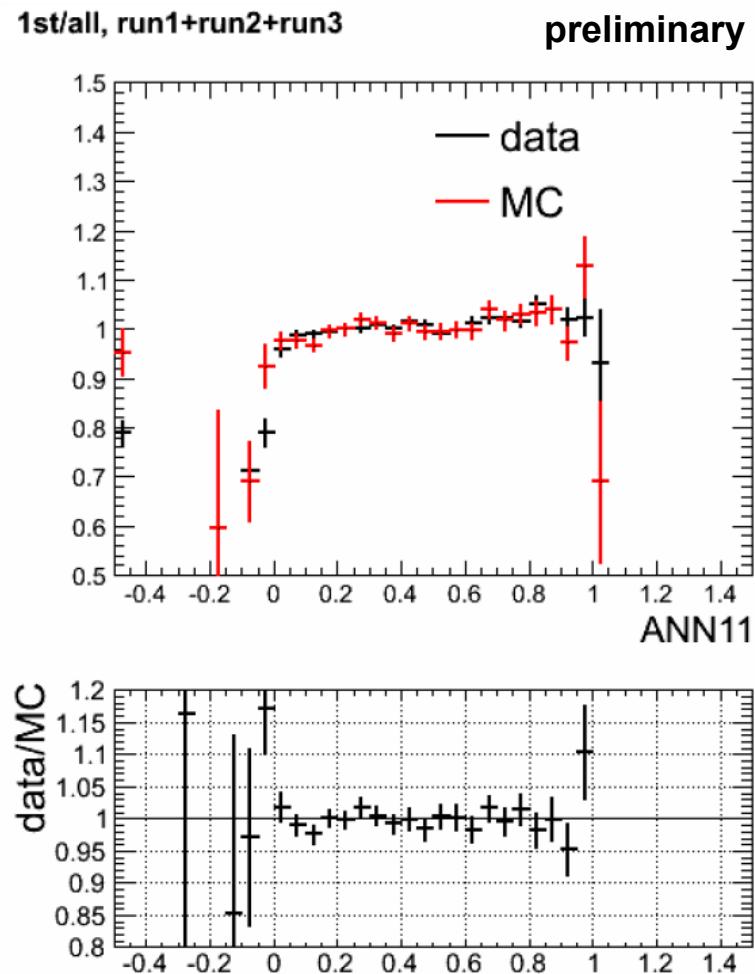
ND data

F/N ratio of MC selected events from component  $\alpha$  in energy bin i

# Beam Intensity Uncertainties

- ND and FD have different beam intensity, and due to the high intensity beam in the ND, there are some late activities and noise.
- We analyze the first event .vs. all the events PID selection efficiency to estimate the intensity systematic error.
- The results shows the intensity effect is modeled quite well.

	ANN11		
	data	mc	data/mc
All Runs			
1 <sup>st</sup> event	$0.117 \pm 0.001$	$0.121 \pm 0.001$	
all events	$0.114 \pm 0.001$	$0.118 \pm 0.000$	
1st/all ratio	$1.027 \pm 0.007$	$1.025 \pm 0.009$	$1.002 \pm 0.011$

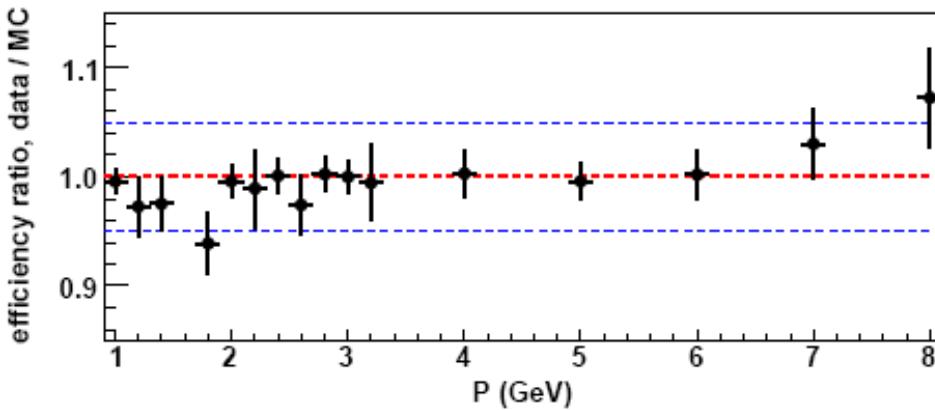
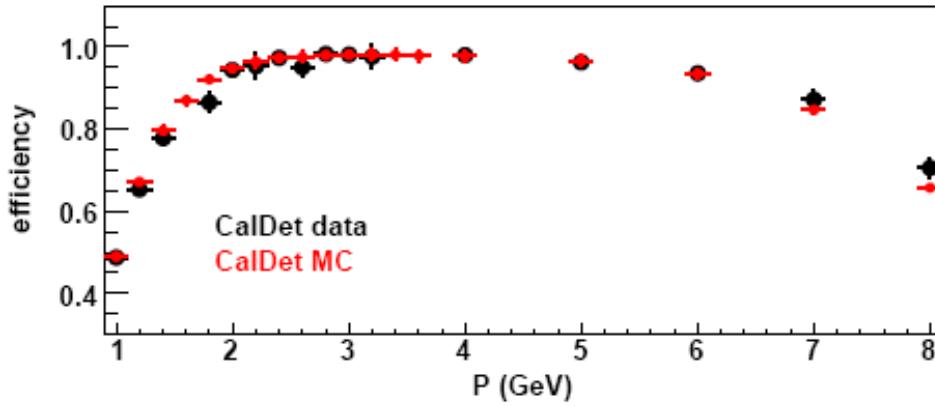


# Background Systematic Uncertainty

Source of Uncertainty	Effect on Background Prediction
ND Decomposition	$\pm 2.8\%$
Calibration	$+2.8\%, -2.3\%$
Far/Near Normalization	$\pm 2.4\%$
Hadronization Model	$\pm 2.3\%$
$\nu_\tau$ CC component	$\pm 1.7\%$
Intranuclear Model	$+0.9\%, -1.0\%$
Beam Model	$\pm 0.5\%$
Crosstalk	$\pm 0.4\%$
Cross Section	$\pm 0.1\%$
<b>Total Background Systematic</b>	<b><math>+5.6\%, -5.3\%</math></b>

**Expected Statistical Uncertainty ~14%**

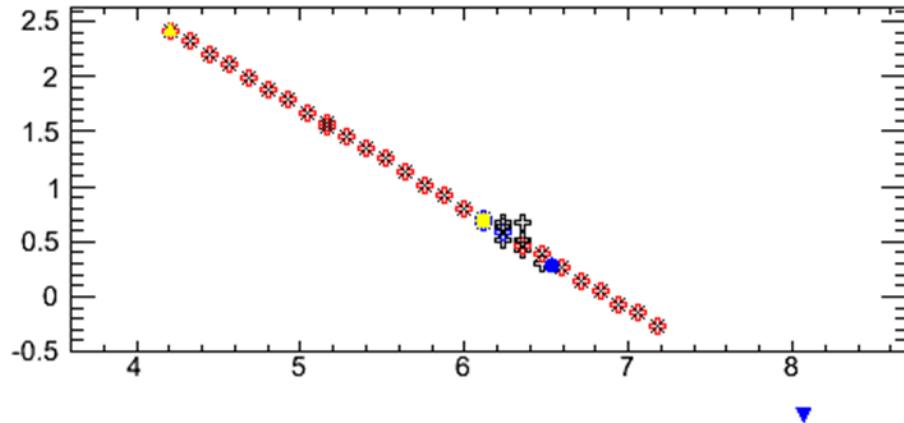
# EM Shower Modeling Check: CalDet Data Sample



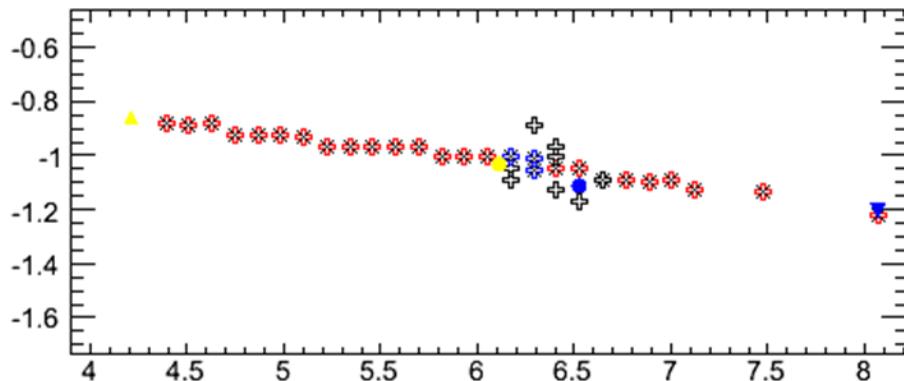
Single electrons are well modeled in the MINOS detector and the selection efficiency agrees with the simulation within 1.6%.

# EM Shower Modeling Check: Cosmic-ray Muon Shower Sample

UZProjection



VZProjection



\* Muon track hits

\* Shared hits

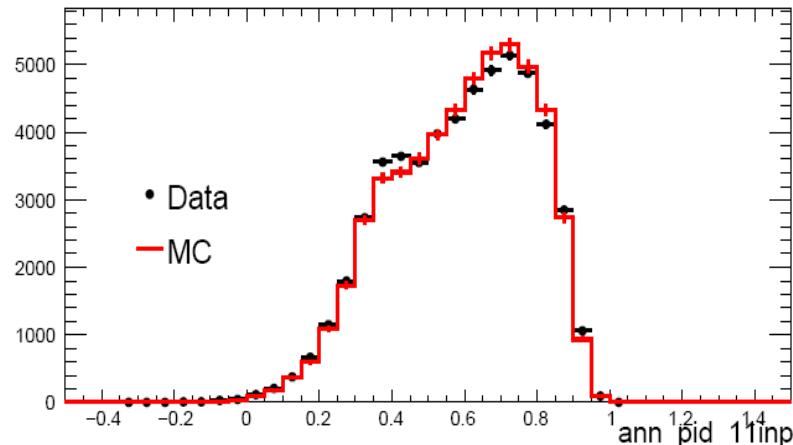
⊕ Retained hits

- Cosmic-ray muon induced bremsstrahlung showers are EM showers.

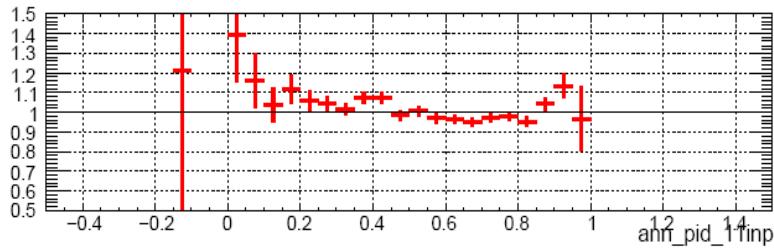
- We can use the cosmic ray showers sample to do the cross check.

# EM Shower Modeling Check: Cosmic-ray Muon Shower Sample

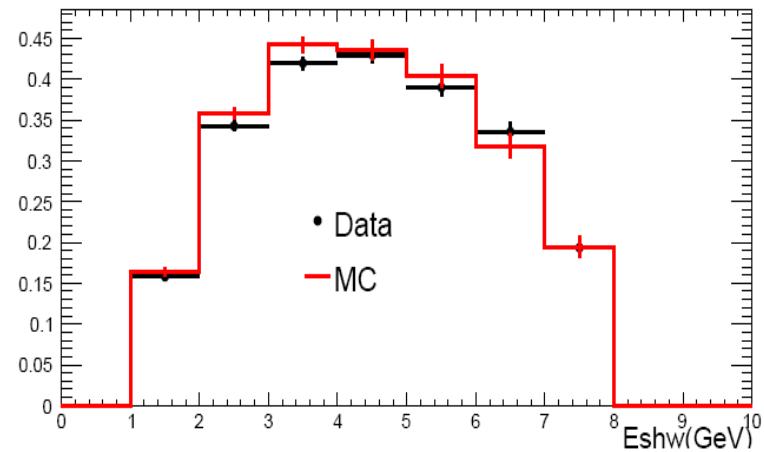
ANN11 PID



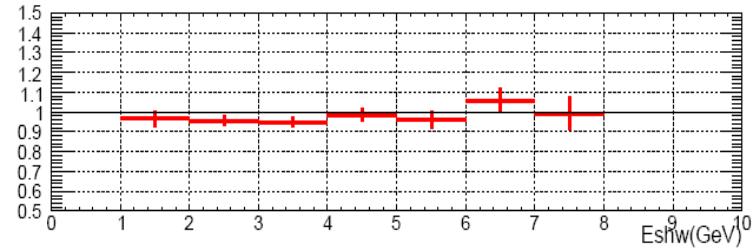
Data/MC



EM Shower Selection Efficiency

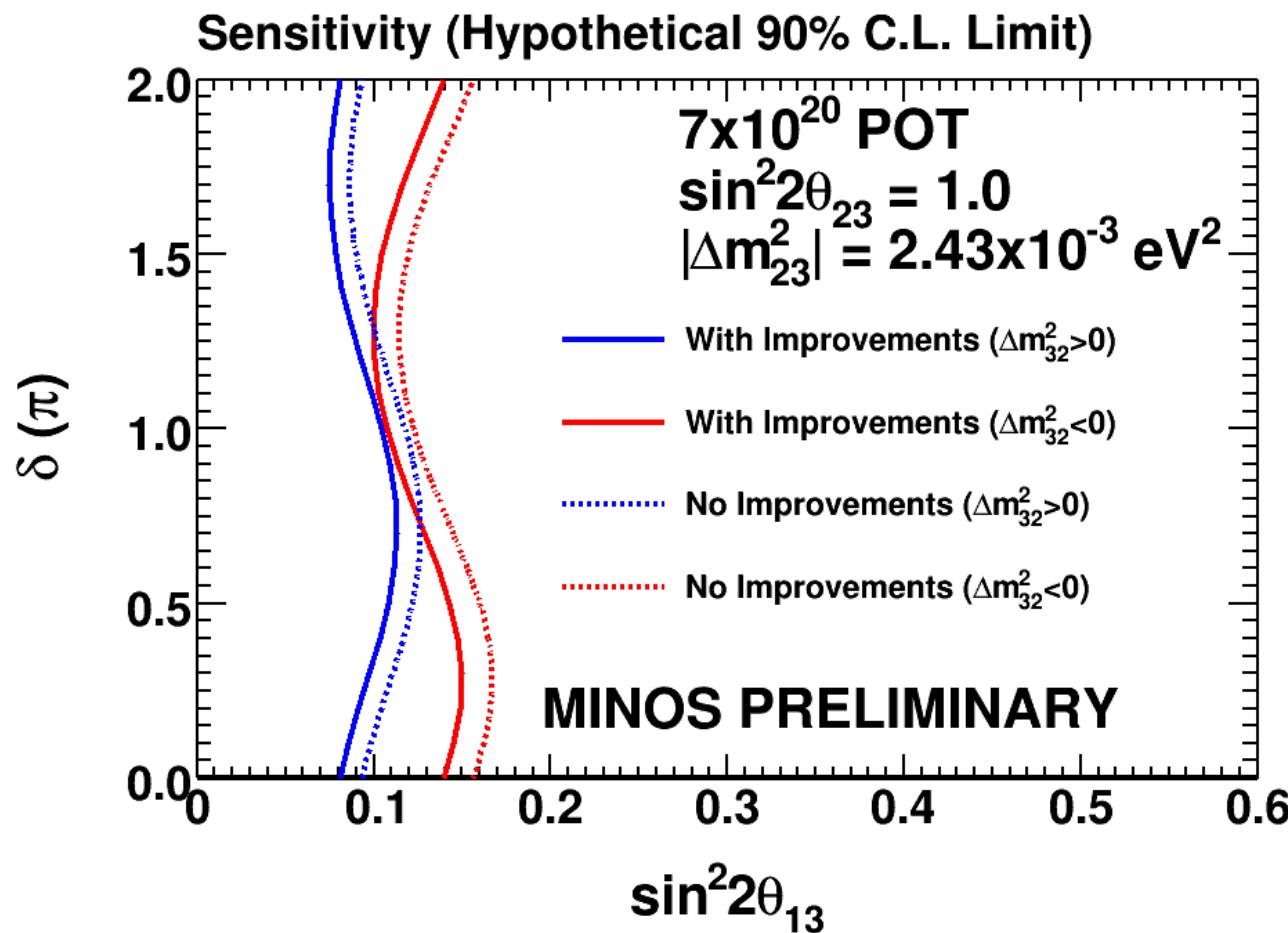


Data/MC



EM shower selection efficiencies of data and MC agree within 5%.

# $\theta_{13}$ Sensitivity



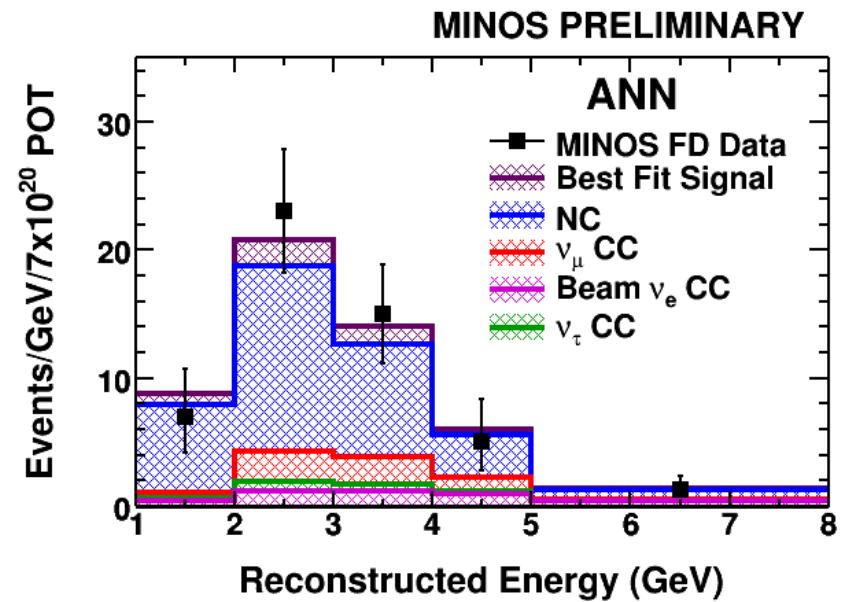
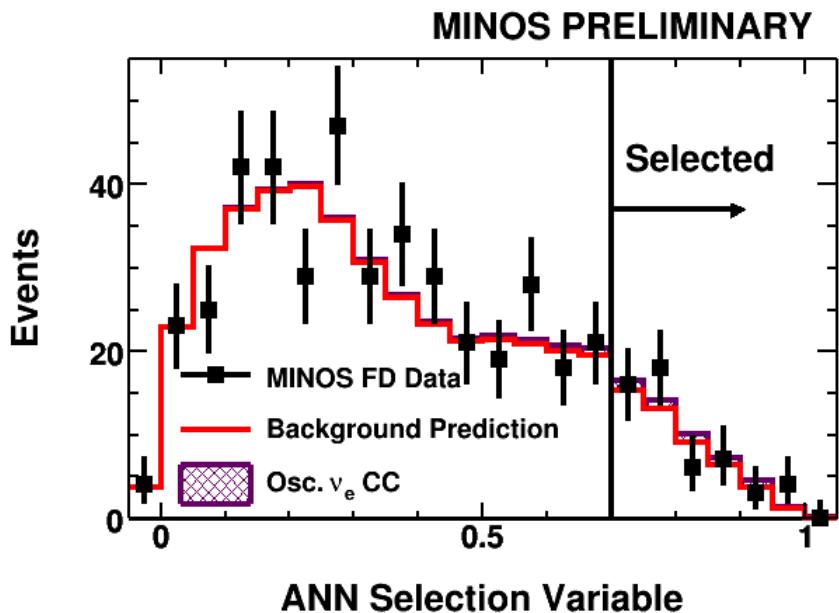
- Retuned ANN with better background rejection
- Improved background decomposition
- Reduced systematic uncertainty ( $7.3\% \rightarrow 5.6\%$ ) with improved MC simulation and event reconstruction

# $\nu_e$ appearance Results

Expected background:  $49.1 \pm 7.0$  (stat)  $\pm 2.7$  (syst)

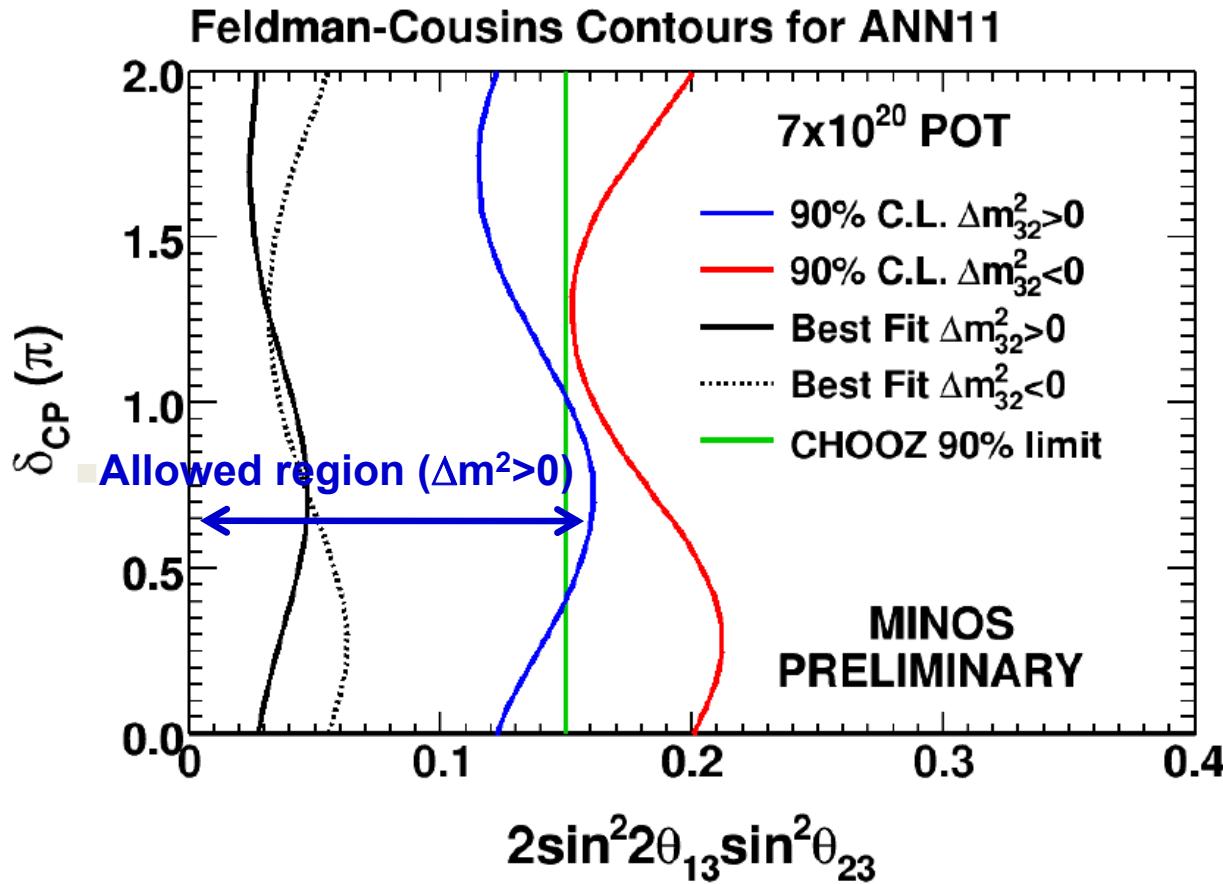
Observation: 54 events,  $0.7\sigma$  more than expectation

If  $\theta_{13}$  is at the CHOOZ limit, we expect 23.7 signal events



- Assuming best fit value of  $\theta_{13}$  at  $\delta=0$ , normal hierarchy

# 90% Upper Limit for $\theta_{13}$



At  $\delta=0$ ,  
 $\sin^2(2\theta_{13}) < 0.12$   
**(normal mass hierarchy)**

$\sin^2(2\theta_{13}) < 0.20$   
**(Inverted mass hierarchy)**

Best Fit:  
 $\sin^2(2\theta_{13}) = 0.027$   
**(normal mass hierarchy)**

$\sin^2(2\theta_{13}) = 0.055$   
**(Inverted mass hierarchy)**

Our 90% C.L. upper limit is beyond the CHOOZ limit assuming normal hierarchy for almost all values of  $\delta$

# Summary

- MINOS data require  $\sin^2(2\theta_{13}) < 0.12(0.20)$  at  $\delta_{cp} = 0$  for normal and inverted hierarchy.
- Remaining questions :
  - Is  $\nu_3$  mostly  $\nu_\mu$  or  $\nu_\tau$ ? ( $\theta_{23} > \pi/4$ ,  $\theta_{23} < \pi/4$ , or  $\theta_{23} = \pi/4$ ?)
  - What is the  $\nu_e$  component of  $\nu_3$ ? ( $\theta_{13} \neq 0$ ?)
  - Is CP-invariance violated in neutrino oscillations? ( $\delta_{cp} \neq 0, \pi$ ?)
  - What is the neutrino mass hierarchy?
  - .....

backup

## Other selection methods

Official selector (ANN11):

*Observed:* 54  
*BG expected:*  $49 \pm 7(\text{stat.}) \pm 3(\text{syst.})$   
*Difference:*  $0.67\sigma$

**All consistent**

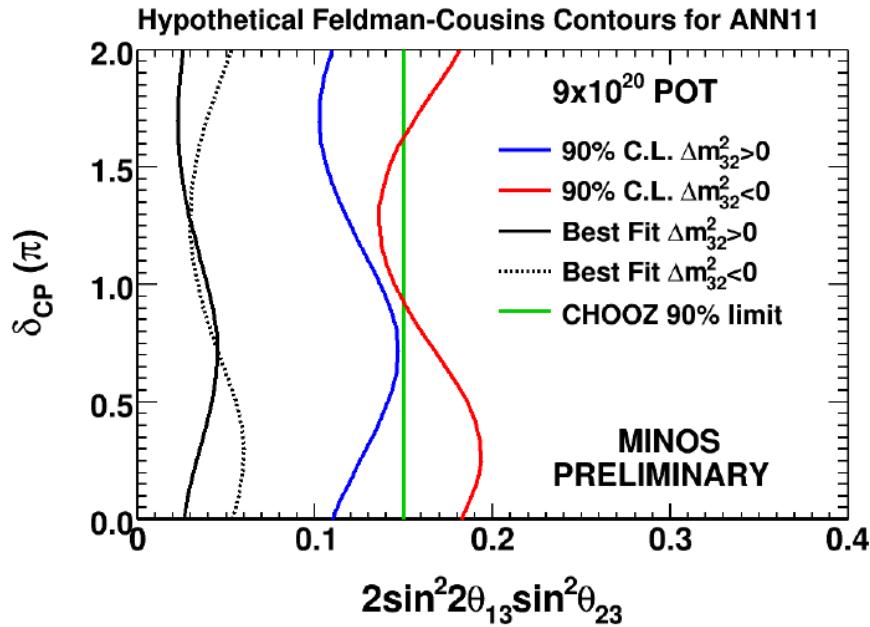
Alternate selector (ANN14):

*Observed:* 36  
*BG expected:*  $34 \pm 6(\text{stat.}) \pm 2(\text{syst.})$   
*Difference:*  $0.35\sigma$

Alternate selector (PAR):

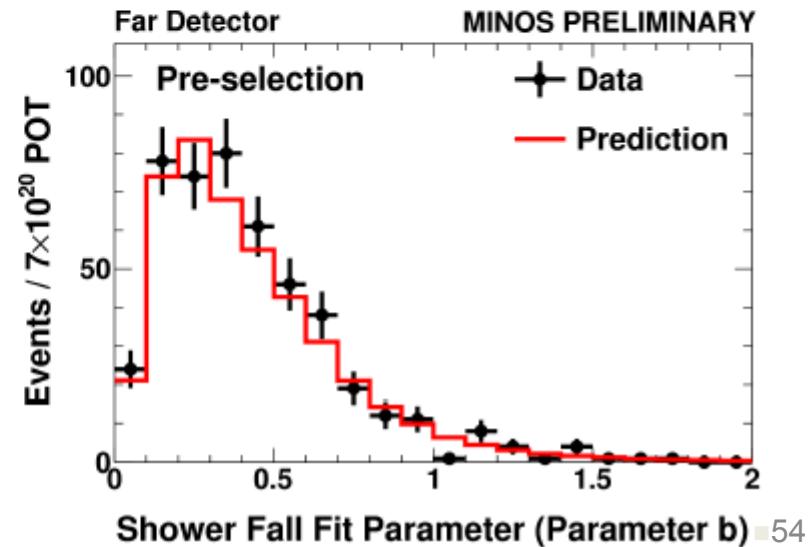
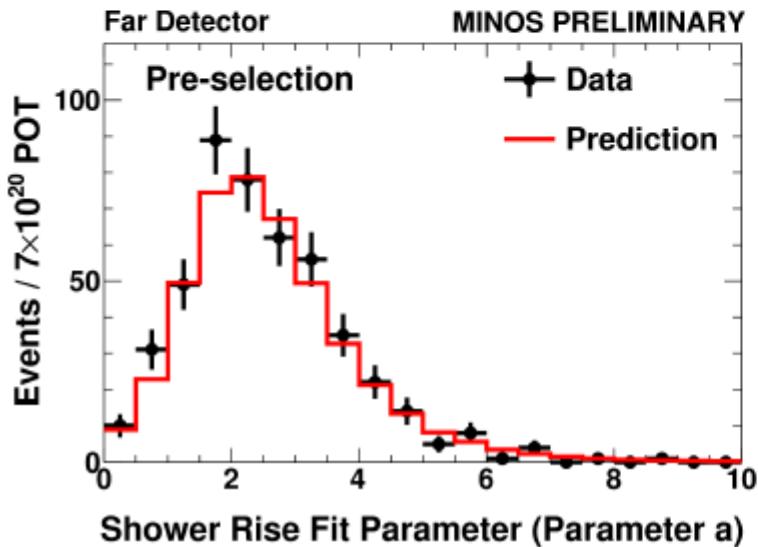
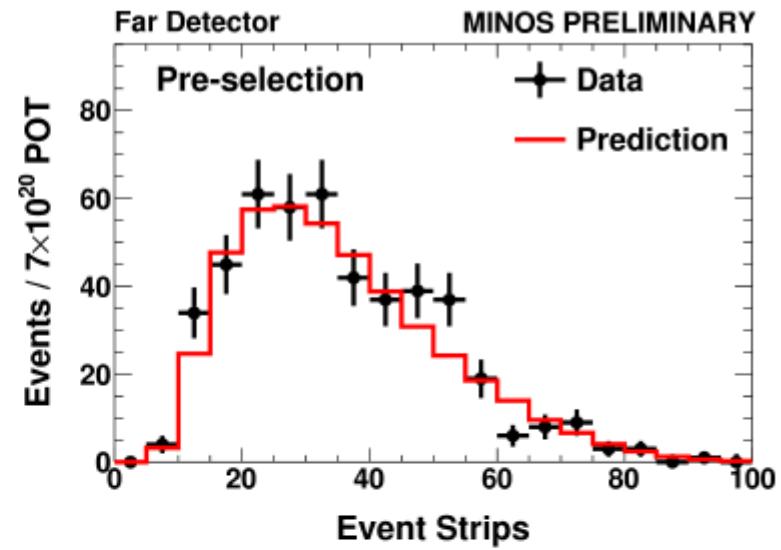
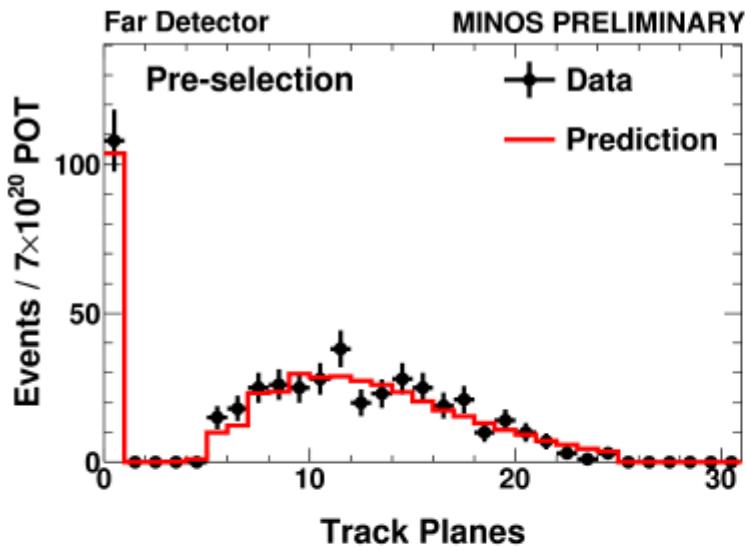
*Observed:* 59  
*BG expected:*  $54 \pm 7(\text{stat.}) \pm 3(\text{syst.})$   
*Difference:*  $0.64\sigma$

# Future

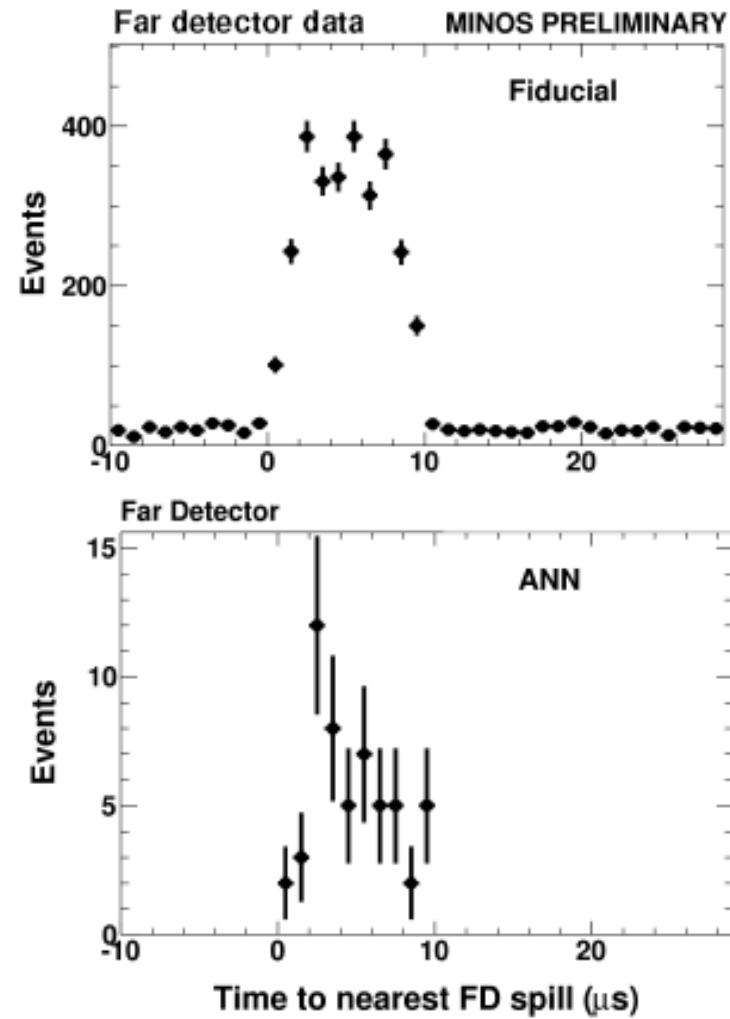
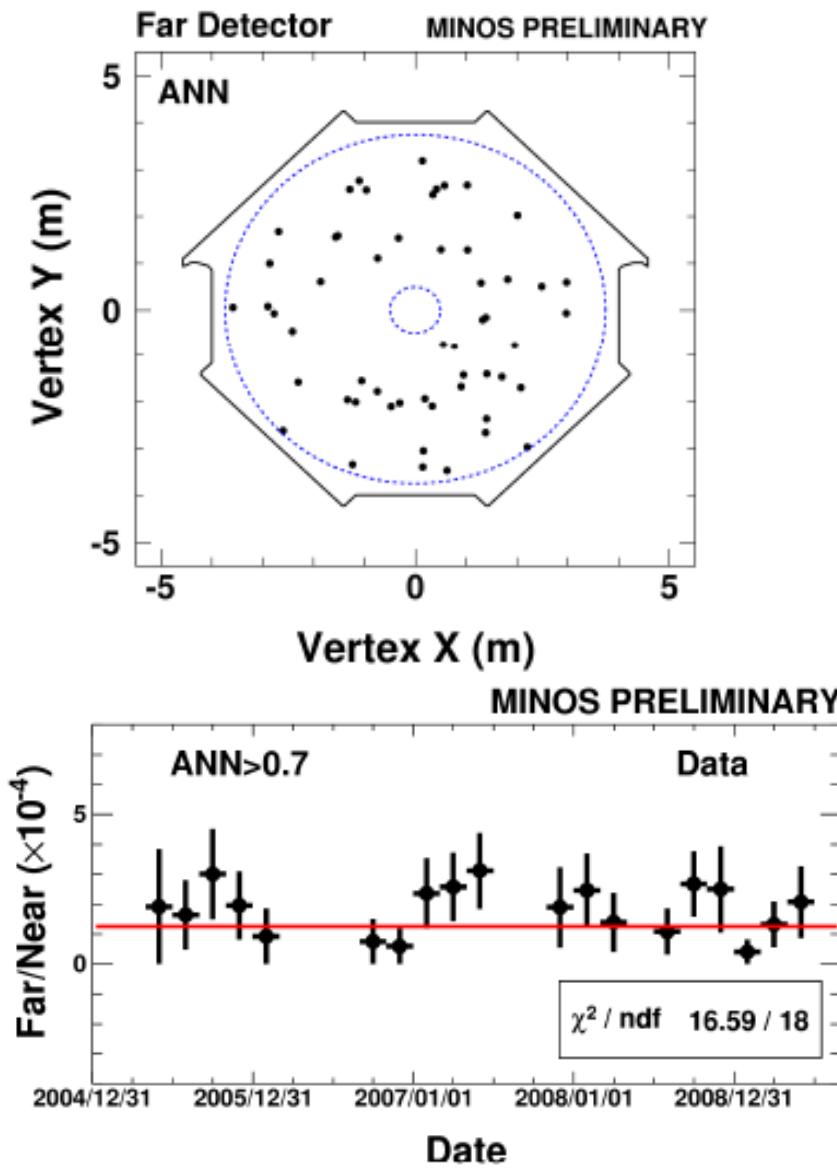


Expected results with  $9 \times 10^{20}$  POT assuming the data excess persists

# Event Shape in the Far Detector



# Position and times



## ANN variables

**Fraction of pulseheight in a n-plane window (n=2,4,6):** the fraction of energy deposited in sliding window of n planes divided by the event energy.

**Fraction of pulseheight in a narrow road:** fraction of total visible energy deposited in a 3 strip window along the shower axis.

**Lateral shower spread (RMS):** the RMS of the transverse energy deposition profile, where the RMS is computed over a 9 strip window around the pulseheight weighted center of the event.

**Radius of 90% energy containment (strips):** the number of strips away from the peak of the transverse energy distribution to contain 90% of the energy deposited in a 9 strip window around the pulseheight weighted center of the event.

**Shower fit raise and fall parameters (a and b):** parameters from the fit to the longitudinal profile of the energy deposition of an event.

**Longitudinal energy projection:** the energy weighted sum of the distance to each strip projected along the detector z axis.

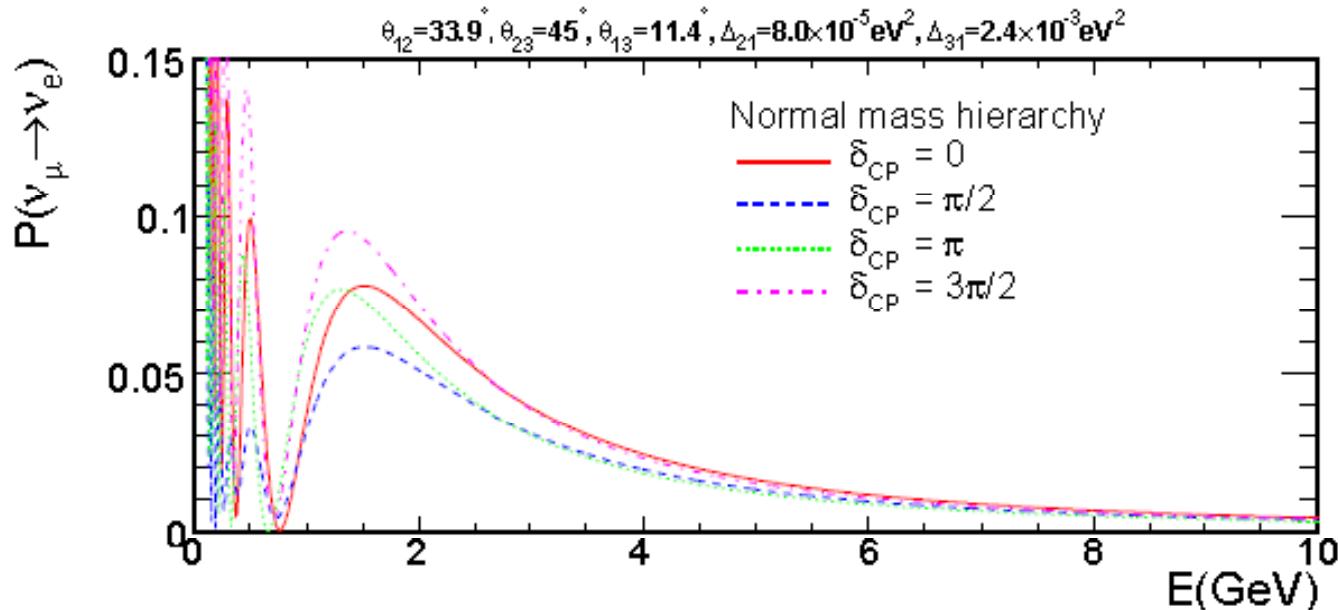
**Minimal spanning tree summed weight:** the sum of the minimum distances that join the hits of larger than average pulseheight hits in an event.

**Fraction of pulseheight in 8 highest PH strips:** the fraction of pulseheight in the highest 8 strips divided by the event energy.

# 3-flavor oscillation

$$\begin{aligned} P(\nu_\mu \rightarrow \nu_e) &= |e^{-i(\Delta_{32} + \delta)} \sin 2\theta_{13} \sin \theta_{23} \sin \Delta_{31} + \sin 2\theta_{12} \cos \theta_{23} \cos \theta_{13} \sin \Delta_{21}|^2 \\ &= \sin^2 \theta_{23} \sin^2 2\theta_{13} \sin^2 \Delta_{31} + \cos^2 \theta_{13} \cos^2 \theta_{23} \sin^2 2\theta_{12} \sin^2 \Delta_{21} \\ &\quad + J_r \sin \Delta_{21} \sin \Delta_{31} \cos(\Delta_{32} + \delta) \\ &= P_{atm} + P_{sol} + P_{int} \end{aligned} \tag{2.7}$$

$$J_r \equiv \sin 2\theta_{12} \sin 2\theta_{23} \sin 2\theta_{13} \cos \theta_{13}$$



# Neutrino Mixing

- The Pontecorvo-Maki-Nakagawa-Sakata (PMNS) matrix can be factorized into 4 experimental regimes:

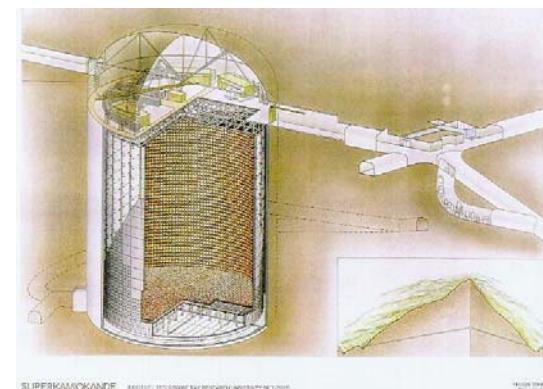
## Atmospheric

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta_{23} & \sin \theta_{23} \\ 0 & -\sin \theta_{23} & \cos \theta_{23} \end{pmatrix} \begin{pmatrix} \cos \theta_{13} & 0 & e^{-i\delta_{CP}} \sin \theta_{13} \\ 0 & 1 & 0 \\ -e^{-i\delta_{CP}} \sin \theta_{13} & 0 & \cos \theta_{13} \end{pmatrix} \begin{pmatrix} \cos \theta_{12} & \sin \theta_{12} & 0 \\ -\sin \theta_{12} & \cos \theta_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} e^{i\alpha_1/2} & 0 & 0 \\ 0 & e^{i\alpha_2/2} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

- (23) Sector identified with atmospheric mixing

- ✓ driven by larger  $|\Delta m^2_{32}| \sim 2.4 \times 10^{-3} \text{ eV}^2$
- ✓  $\theta_{23} \sim 45^\circ$  (Is it maximal?)
- ✓ experiments with  $L/E \sim 500 \text{ km/GeV}$

[SuperK, K2K, MINOS]



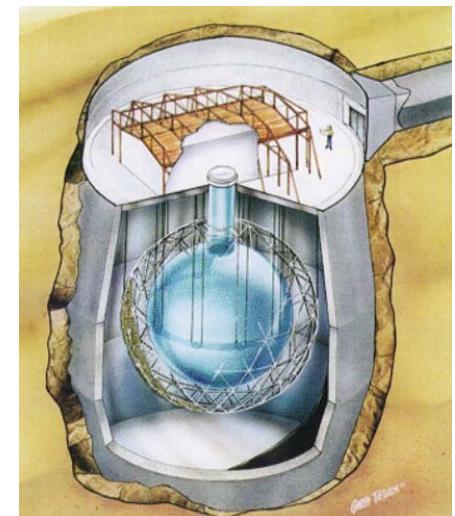
SuperK

# Neutrino Mixing

- The Pontecorvo-Maki-Nakagawa-Sakata (PMNS) matrix can be factorized into 4 experimental regimes:

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta_{23} & \sin \theta_{23} \\ 0 & -\sin \theta_{23} & \cos \theta_{23} \end{pmatrix} \begin{pmatrix} \cos \theta_{13} & 0 & e^{-i\delta_{CP}} \sin \theta_{13} \\ 0 & 1 & 0 \\ -e^{-i\delta_{CP}} \sin \theta_{13} & 0 & \cos \theta_{13} \end{pmatrix} \boxed{\begin{pmatrix} \cos \theta_{12} & \sin \theta_{12} & 0 \\ -\sin \theta_{12} & \cos \theta_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}} \begin{pmatrix} e^{i\alpha_1/2} & 0 & 0 \\ 0 & e^{i\alpha_2/2} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

- (12) Sector identified with solar mixing
  - ✓ driven by small  $\Delta m^2_{21} \sim 7.6 \times 10^{-5} \text{ eV}^2$  and moderately large  $\theta_{12} \sim 34^\circ$
  - ✓ Reactor + Solar experiments at L/E  $\sim 15,000 \text{ km/GeV}$   
[SNO/Kamland]



# Neutrino Mixing

- The Pontecorvo-Maki-Nakagawa-Sakata (PMNS) matrix can be factorized into 4 experimental regimes:

Cross-mixing

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta_{23} & \sin \theta_{23} \\ 0 & -\sin \theta_{23} & \cos \theta_{23} \end{pmatrix} \boxed{\begin{pmatrix} \cos \theta_{13} & 0 & e^{-i\delta_{CP}} \sin \theta_{13} \\ 0 & 1 & 0 \\ -e^{-i\delta_{CP}} \sin \theta_{13} & 0 & \cos \theta_{13} \end{pmatrix}} \begin{pmatrix} \cos \theta_{12} & \sin \theta_{12} & 0 \\ -\sin \theta_{12} & \cos \theta_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} e^{i\alpha_1/2} & 0 & 0 \\ 0 & e^{i\alpha_2/2} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

- (13) Sector mixing not yet observed
  - ✓  $\theta_{13}$  is small ( $\theta_{13} < 10^\circ$  at 90% C.L.)
  - ✓ Reactor experiment (CHOOZ/Palo Verde) + accelerator experiments L/E  $\sim 500\text{km}/\text{GeV}$  (K2K/MINOS)
  - ✓ Is  $\theta_{13}$  zero? (Double CHOOZ / Daya bay)
  - ✓ Is there CP violation in the lepton sector?  
(next generation experiments: T2K/Nova/LBNE)



■ Daya bay

■ 60

# Neutrino Mixing

- The Pontecorvo-Maki-Nakagawa-Sakata (PMNS) matrix can be factorized into 4 experimental regimes:

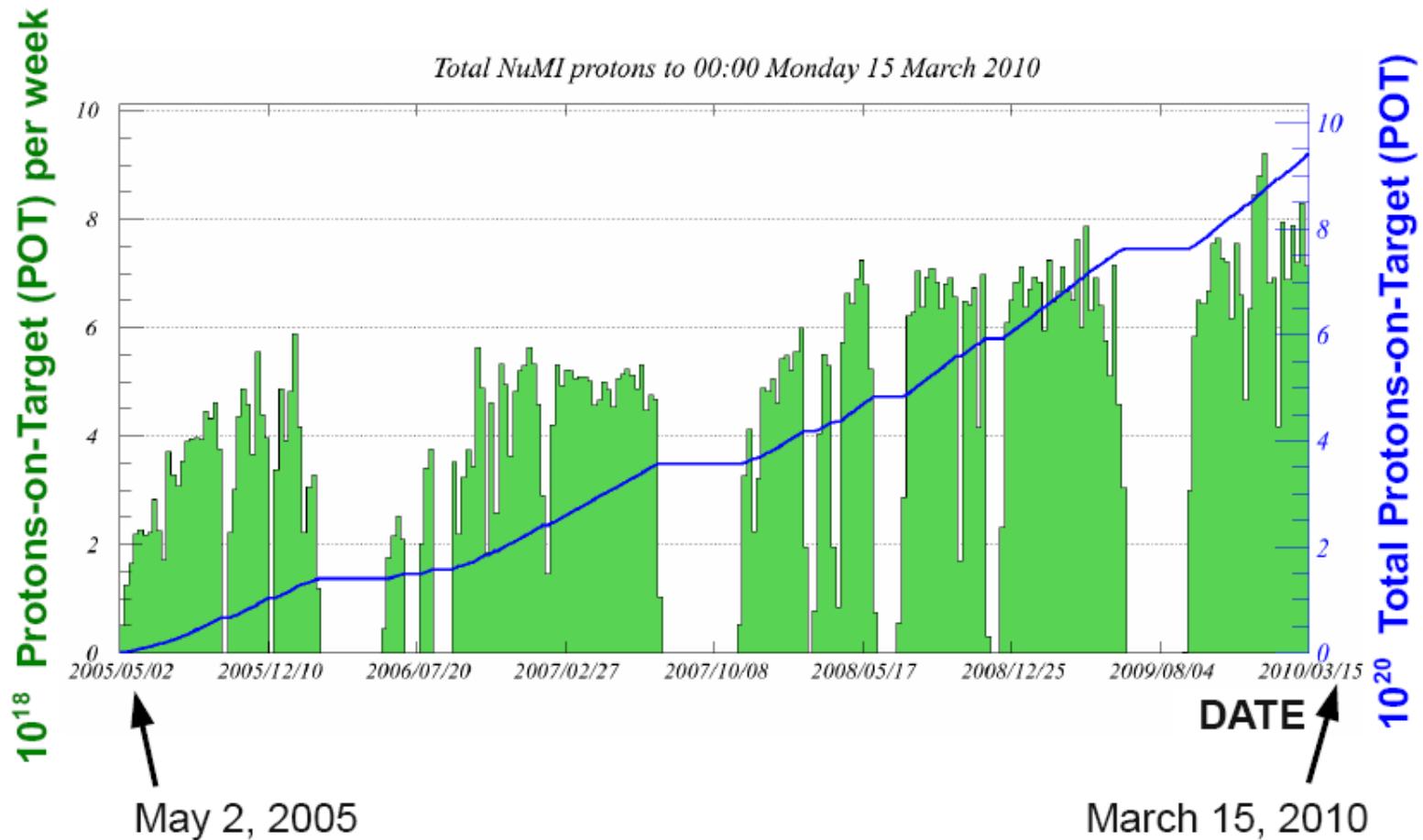
$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta_{23} & \sin \theta_{23} \\ 0 & -\sin \theta_{23} & \cos \theta_{23} \end{pmatrix} \begin{pmatrix} \cos \theta_{13} & 0 & e^{-i\delta_{CP}} \sin \theta_{13} \\ 0 & 1 & 0 \\ -e^{-i\delta_{CP}} \sin \theta_{13} & 0 & \cos \theta_{13} \end{pmatrix} \begin{pmatrix} \cos \theta_{12} & \sin \theta_{12} & 0 \\ -\sin \theta_{12} & \cos \theta_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} e^{i\alpha_1/2} & 0 & 0 \\ 0 & e^{i\alpha_2/2} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

- Majorana phases
  - ✓ two majorana phases are not observable in the oscillation experiments.
  - ✓ They can only be measured by Neutrinoless double beta decay experiments.
  - ✓ Remaining questions: Dirac neutrino or Majorana neutrino?



# Some Remaining Physics Questions

- Is  $\nu_3$  mostly  $\nu_\mu$  or  $\nu_\tau$ ? ( $\theta_{23} > \pi/4$ ,  $\theta_{23} < \pi/4$ , or  $\theta_{23} = \pi/4$ ?)
- What is the  $\nu_e$  component of  $\nu_3$ ? ( $\theta_{13} \neq 0$ ?)
- Is CP-invariance violated in neutrino oscillations? ( $\delta_{cp} \neq 0, \pi$ ?)
- What is the neutrino mass hierarchy?
  - All of these can be addressed in neutrino oscillation experiments if we get lucky, that is  $\theta_{13}$  is large enough.
  - Mass-driven neutrino oscillations lead to a new picture of lepton sector of the standard model.

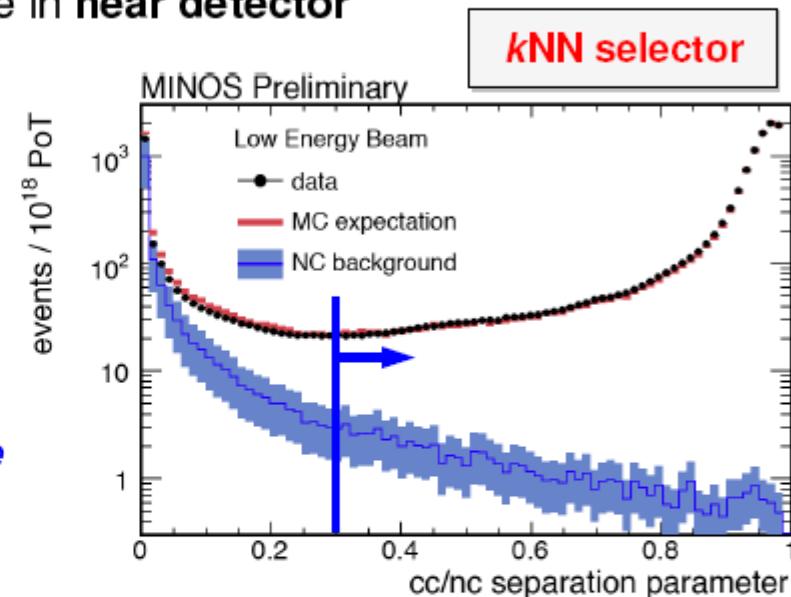


# Muon neutrino disappearance

- Start by measuring  $\nu_\mu$  charged current rate in **near detector**

- Selection:*

- **Fiducial volume** (below)
- Beam timing, cosmic removal
- How “track-like” is the event? – a **k-nearest-neighbors** algorithm using:  
*track length*  
*mean pulse height in each place*  
*fluctuation in pulse heights*  
*transverse track profile*



## Near det.



## Far det.



**Fiducial regions  
(in red)**

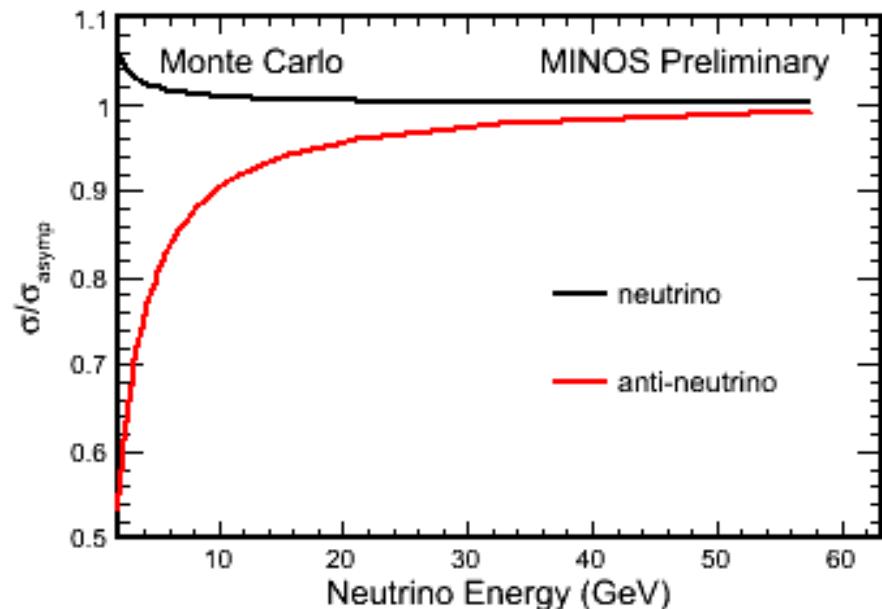
# $v_0$ Correction

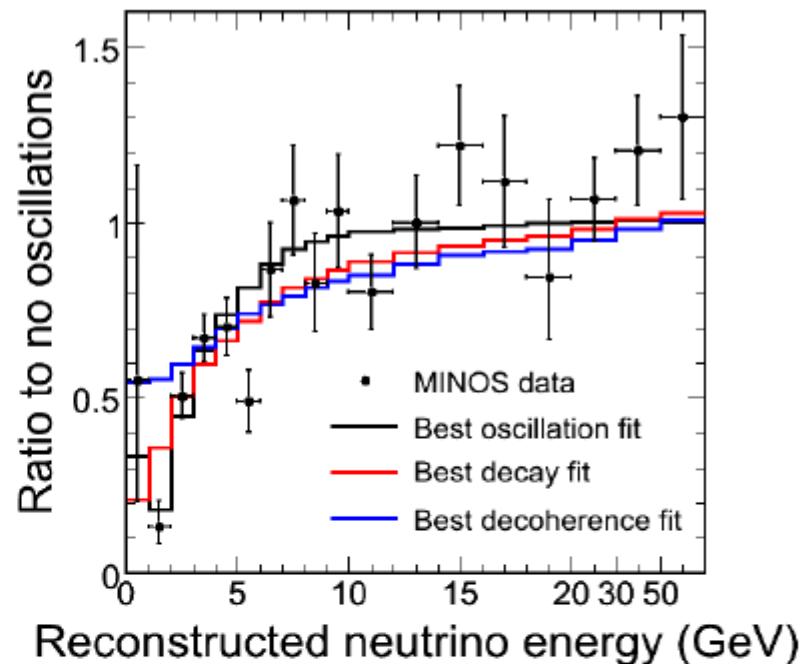
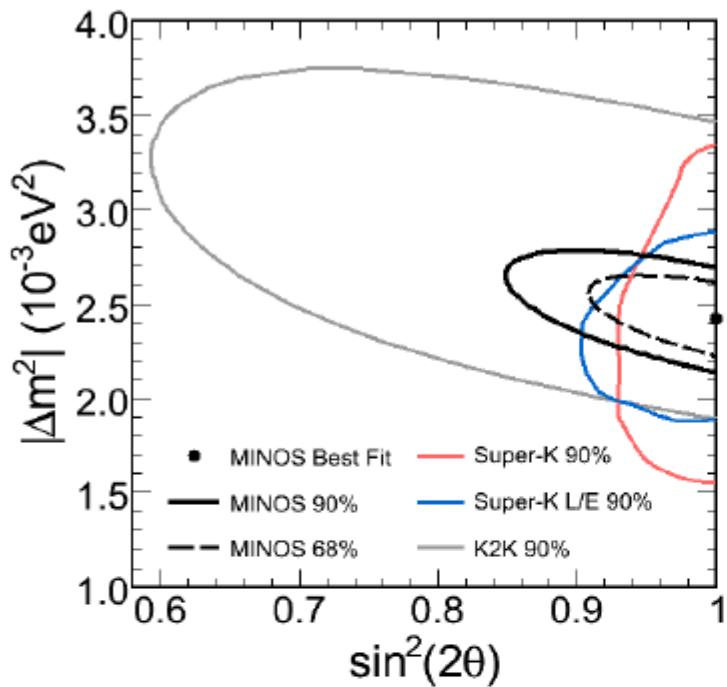
$$\Phi \propto \frac{N(E)_{(v \leq v_0)}}{\int_0^{v_0} \left( 1 + \frac{B}{A} \frac{v}{E} - \frac{C}{A} \frac{v^2}{2E^2} \right) d v}$$

With small but finite  $v_0$ , we need to take the low- $v$  correction, which is calculated with the *NEUGEN* xsection model.

- Advantage:
  - Only dependent on the neutrino interaction cross-section which can be derived without invoking the nucleon structure and type of interactions: scaling(DIS) or non-scaling (QE/RES) process.
- Disadvantage:
  - Sensitive to the muon momentum scale

Low  $v$  correction ( $v < 1$  GeV)





## Oscillation interpretation:

- Parameter space shown above.
- Most precise  $\Delta m_{\text{atm}}^2$  measurement:

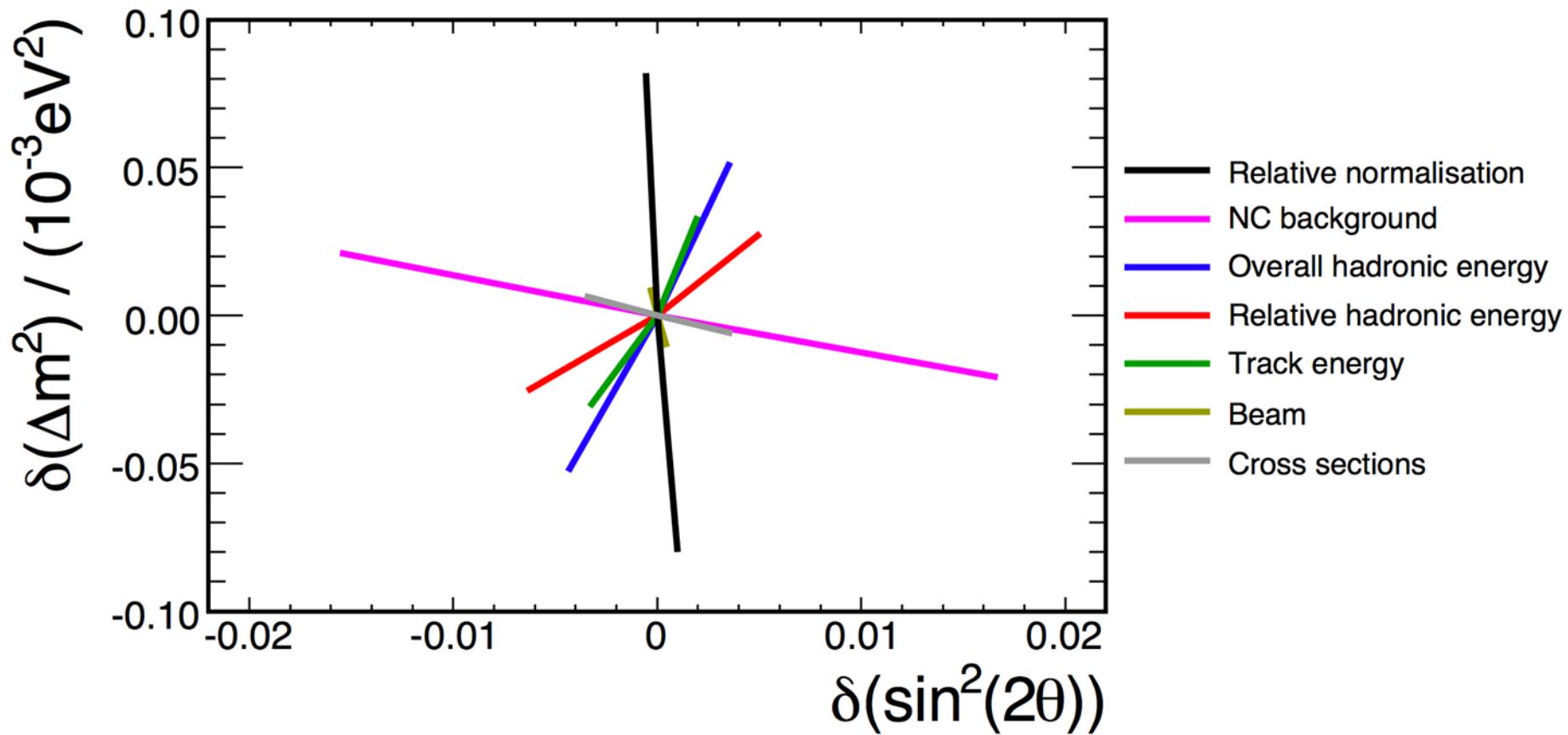
$$\Delta m_{\text{atm}}^2 = (2.43 \pm 0.13) \times 10^{-3} \text{ eV}^2$$

(Uses 3.36 protons-on-target. More than twice this has been collected.)

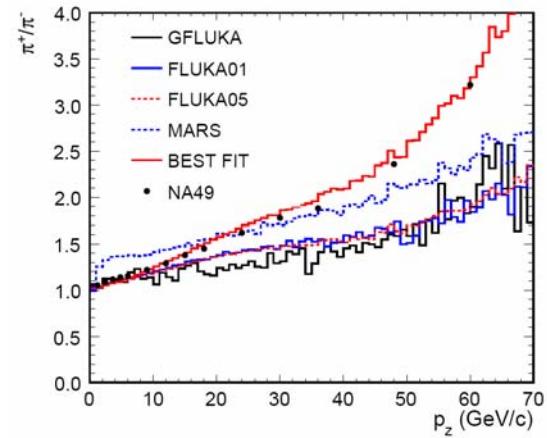
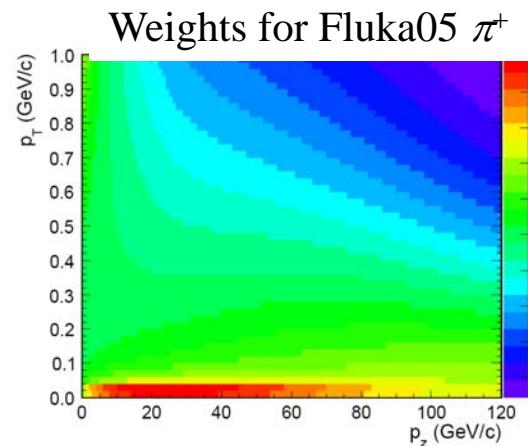
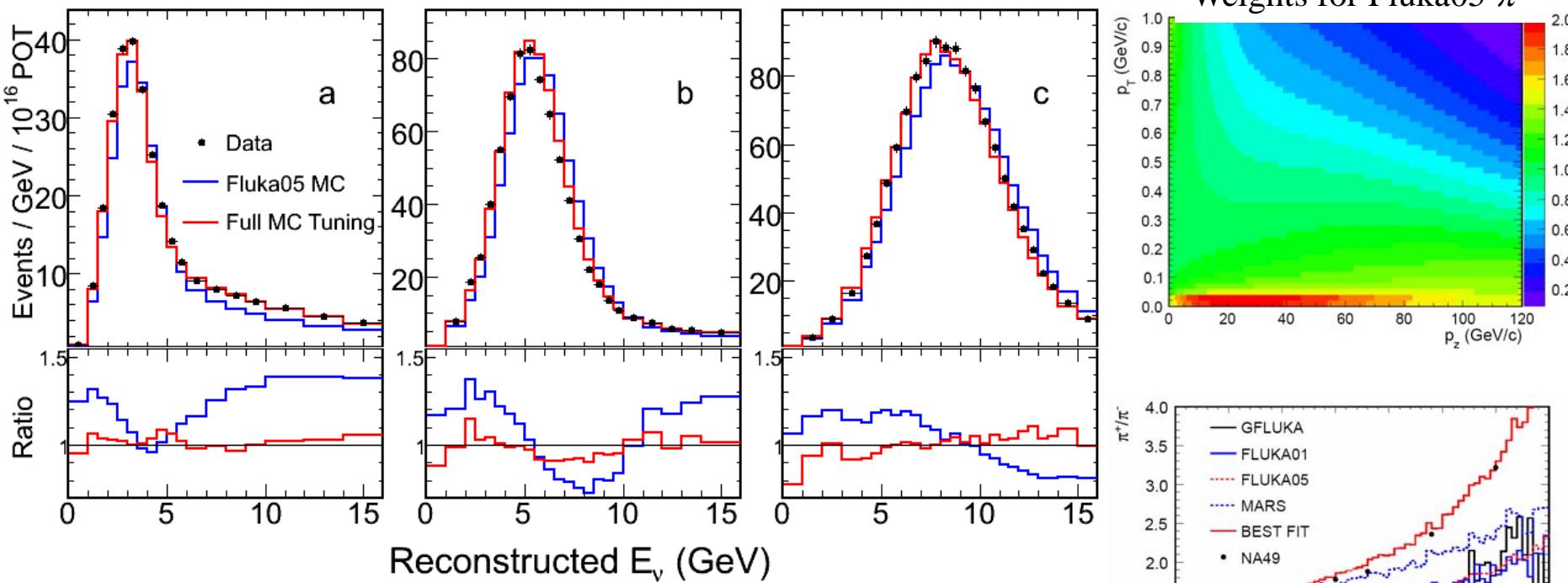
*Strongly disfavored  
alternative interpretations:*

- Neutrino decay:  $3.7\sigma$   
( $5.4\sigma$  with NC sample)
- Decoherence:  $5.7\sigma$

# CC Systematic Uncertainties

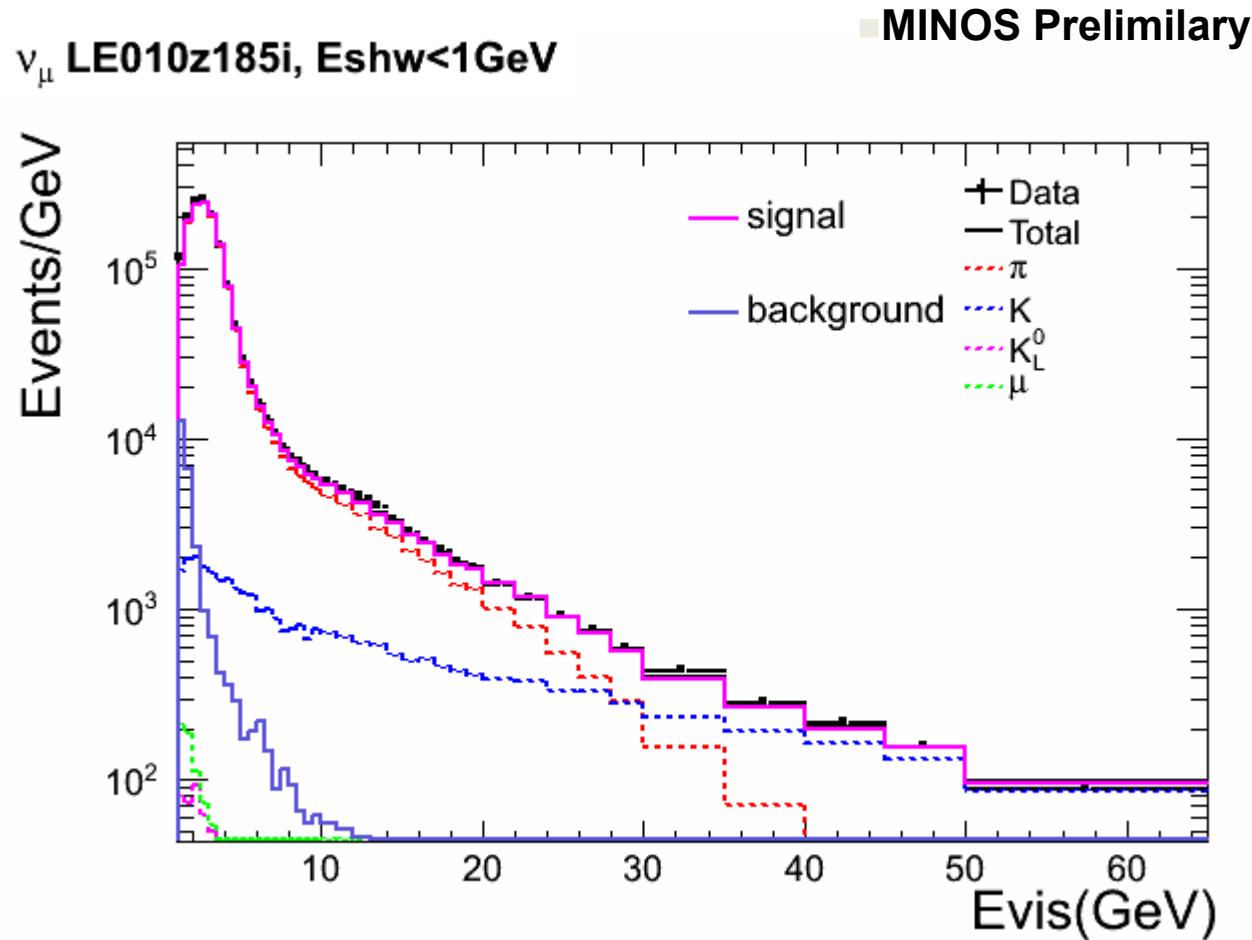


# Standard Hadron Production Tuning



- 3 different beam configurations
- Same hadron production, different focusing
- Default hadron simulation: Fluka05
- Tune hadron production to improve data/MC agreement

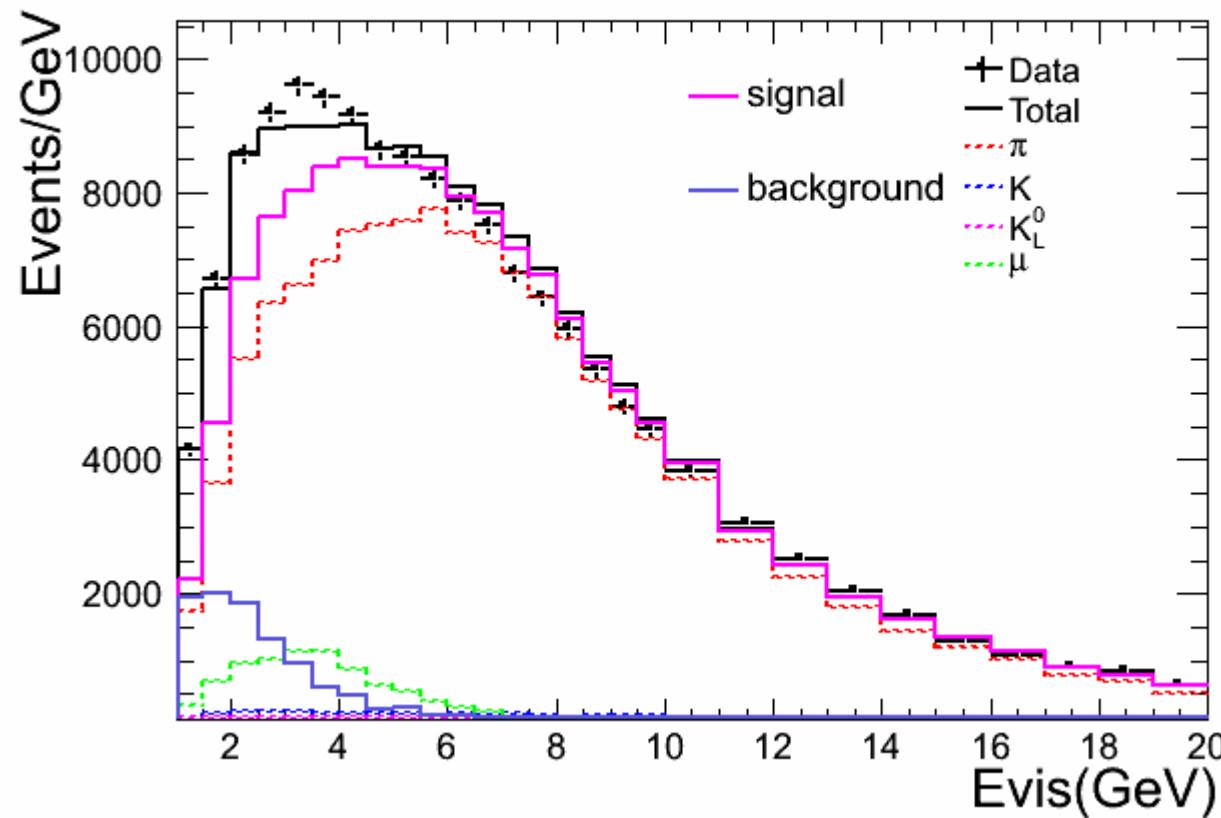
# $\nu_\mu$ low-nu data sample composition

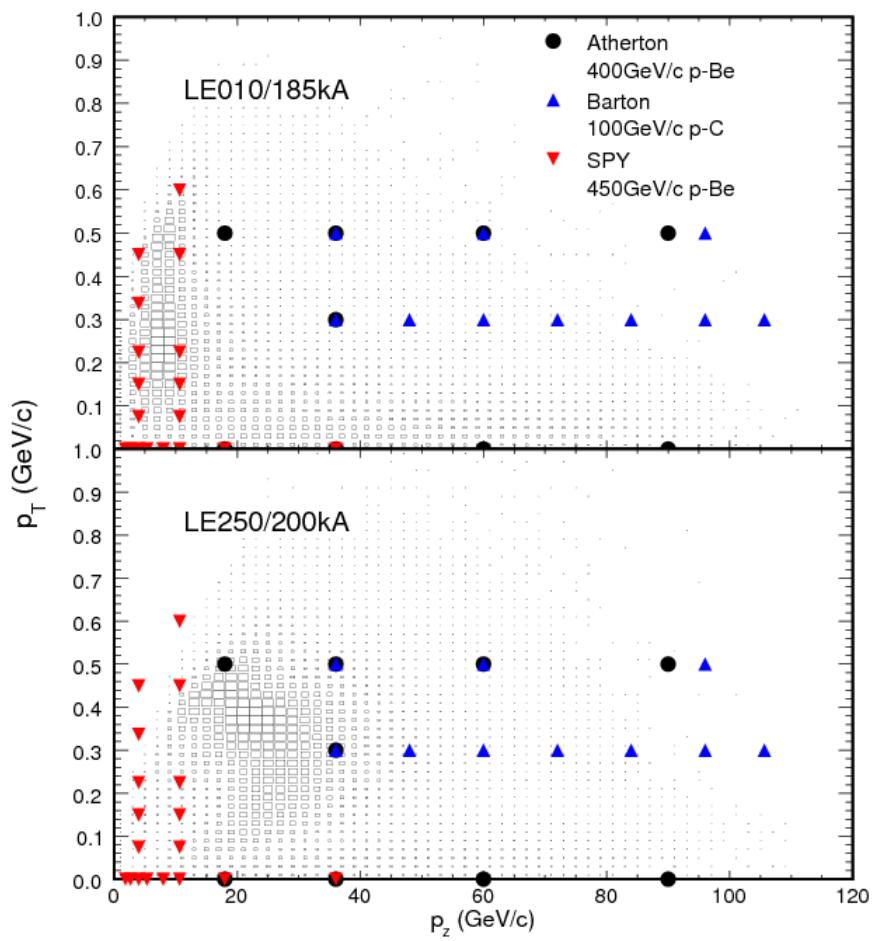
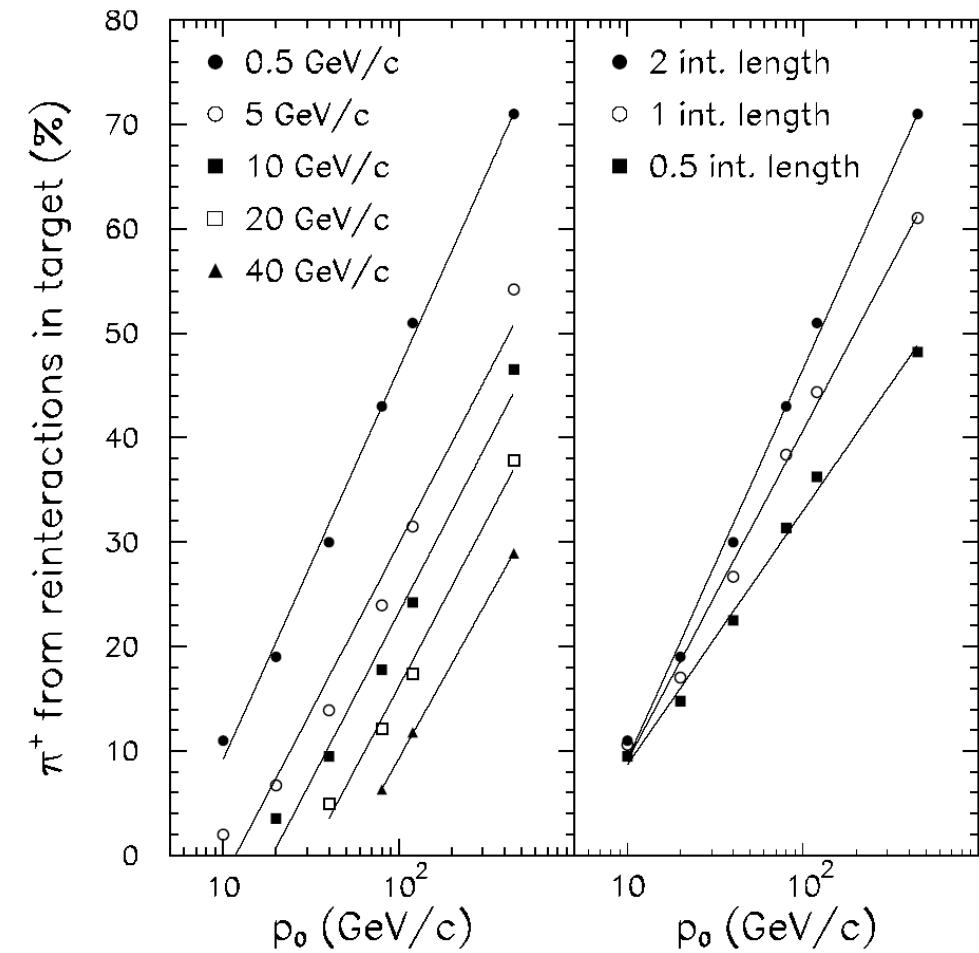


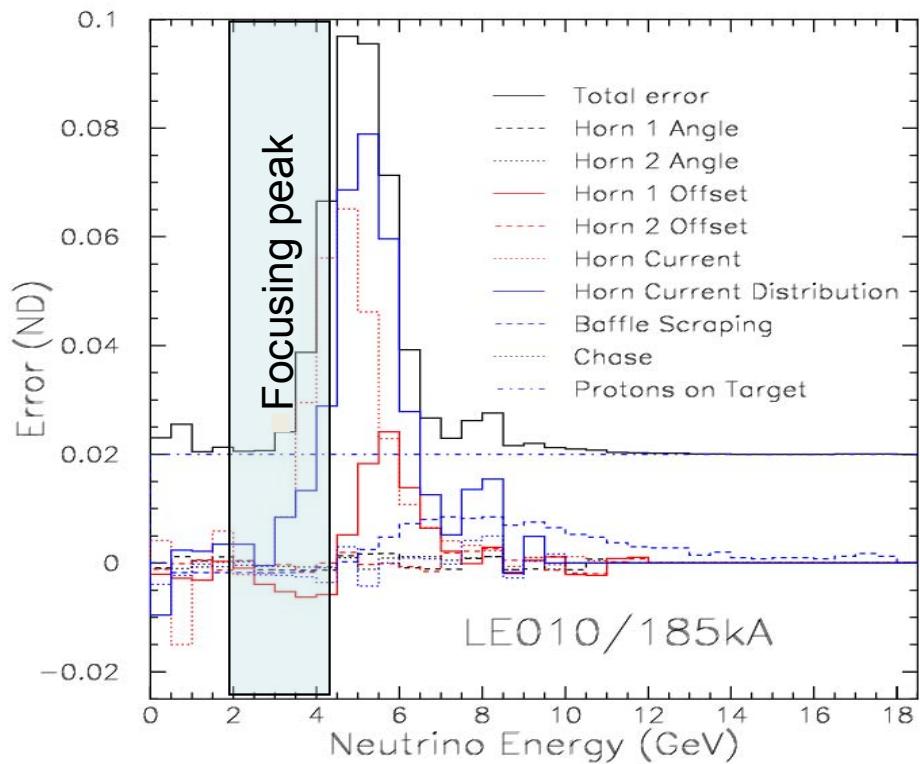
# Anti- $\nu_\mu$ low-nu data sample composition

MINOS Preliminary

$\bar{\nu}_\mu$  LE010z185i, Eshw<1GeV



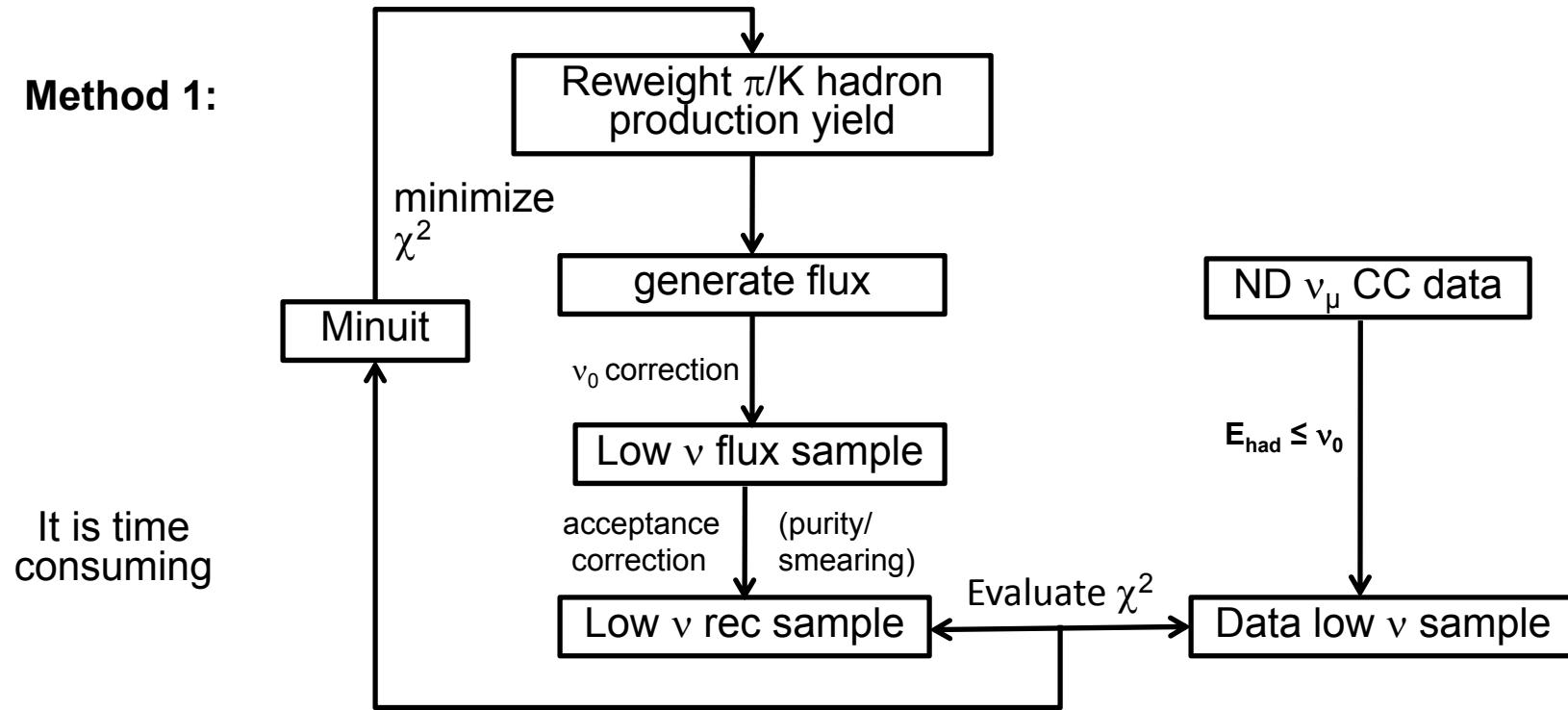




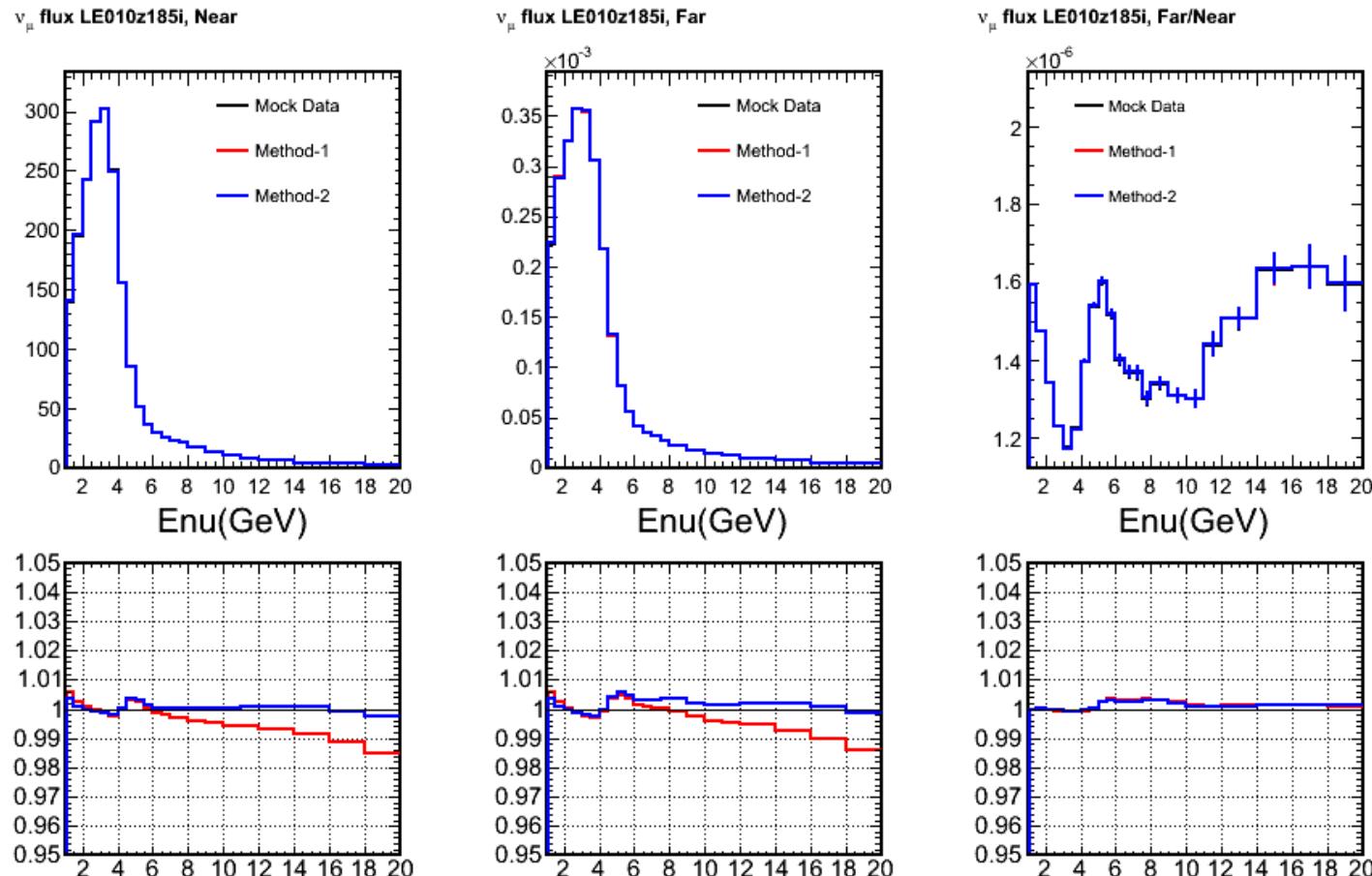
# Empirical Parameterization (EP) Method

- In order to predict the neutrino flux in the Far Detector and estimate the FD/ND flux ratio, we need to parameterize the  $\pi/K$  mesons by using the low-nu flux sample.

**Method 1:**



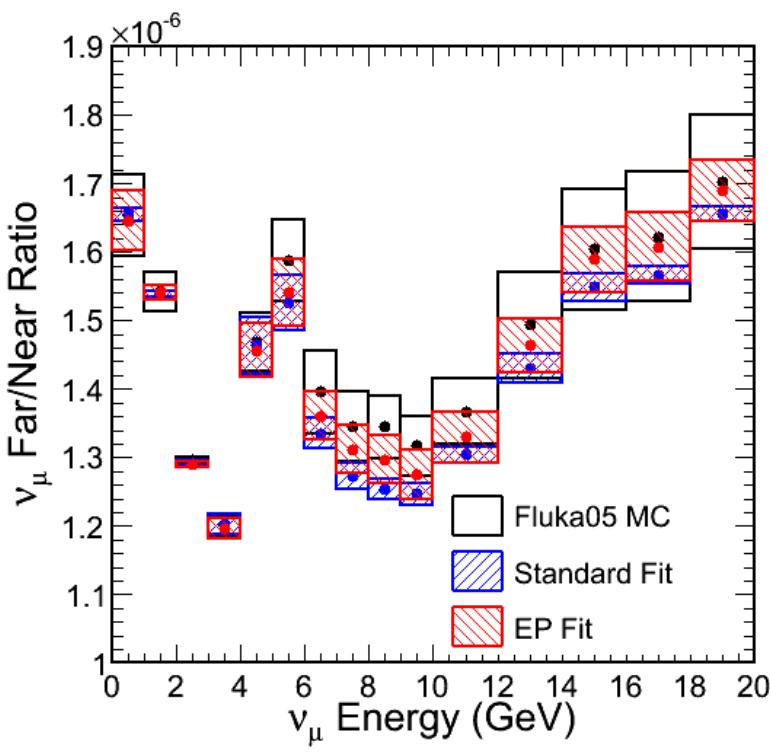
# Mock Data Study



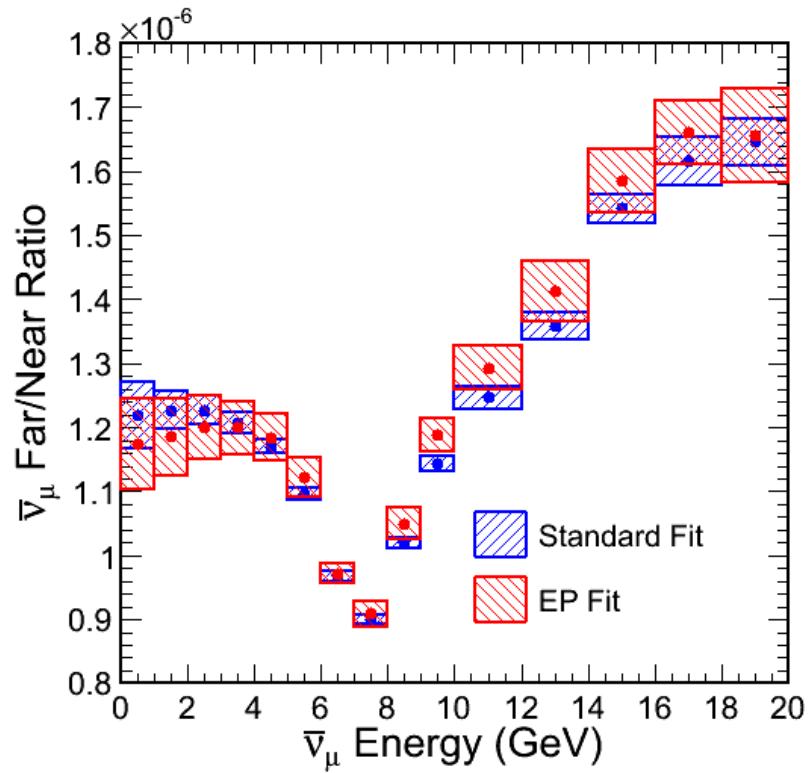
■ Method 1 and Method 2 are equivalent.

# Far/Near Ratio

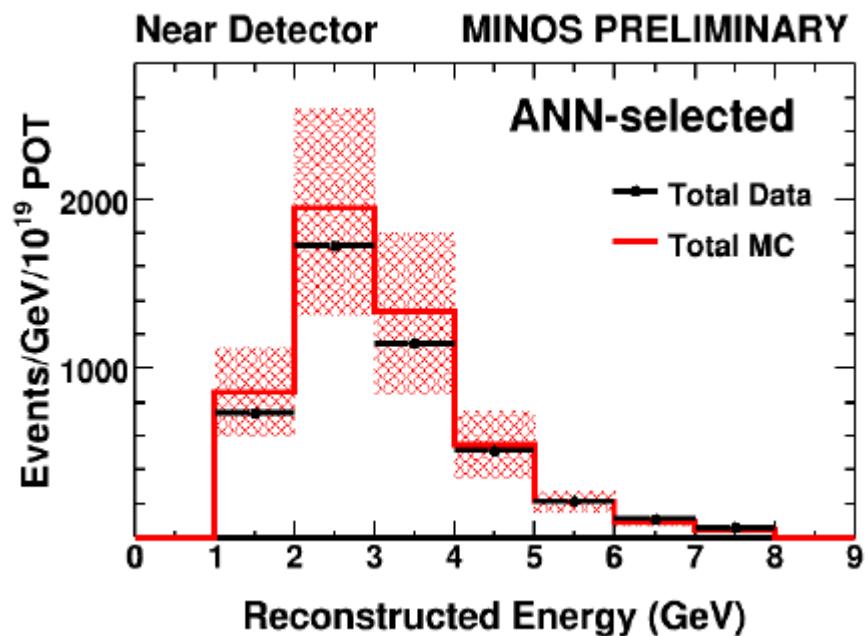
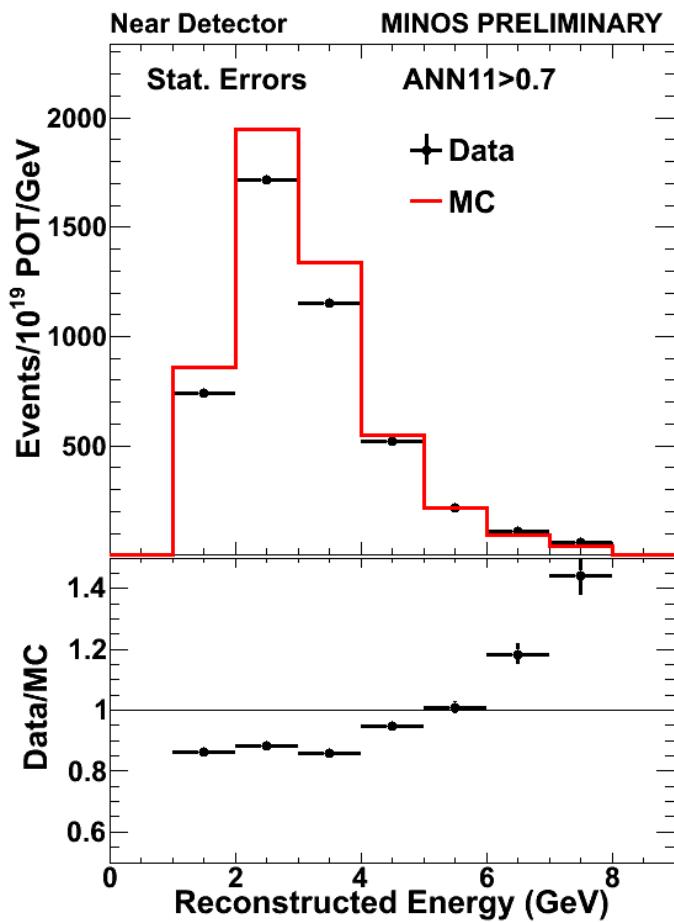
MINOS Preliminary



MINOS Preliminary



# Background of ND data



# ND Decomposition

- There are large uncertainties in our hadronization model. Monte Carlo can't be trusted to determine the background components.
- We can use 3 different beam configurations to do the ND background decomposition. They have different NC/CC/beam  $\nu_e$  composition.

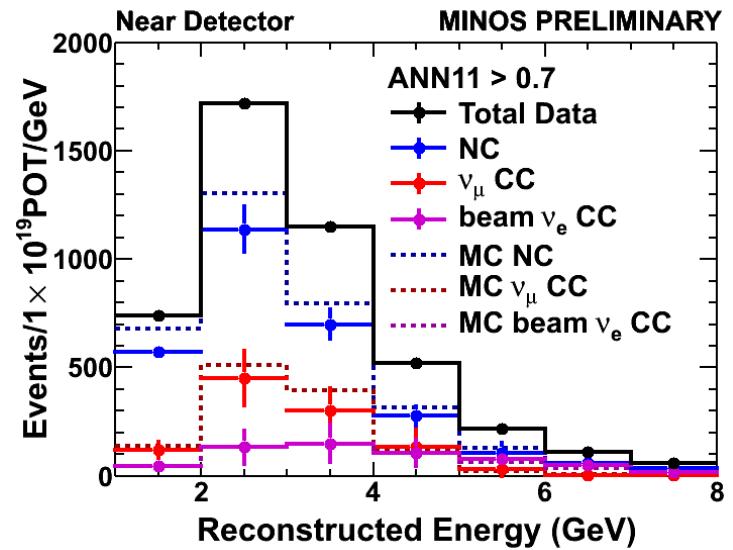
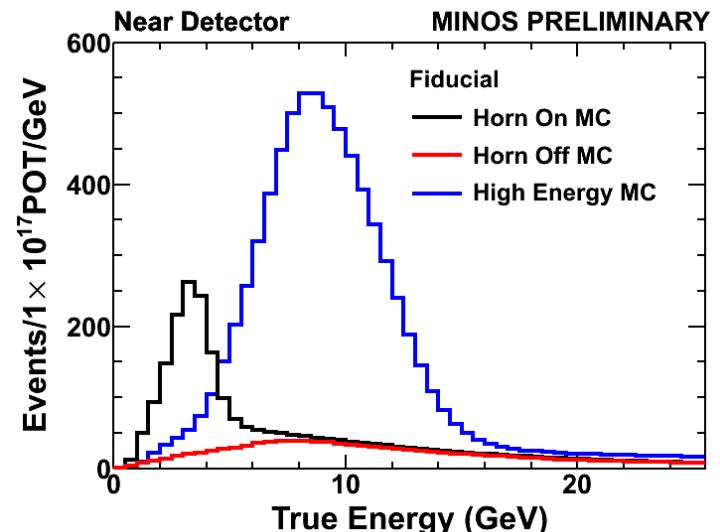
$$N_{NC} + N_{CC} + N_{\nu_e} = N_{data}^{ON}$$

$$\frac{N_{NC}^{OFF\ MC}}{N_{NC}^{ON\ MC}} N_{NC} + \frac{N_{CC}^{OFF\ MC}}{N_{CC}^{ON\ MC}} N_{CC} + \frac{N_{\nu_e}^{OFF\ MC}}{N_{\nu_e}^{ON\ MC}} N_{\nu_e} = N_{data}^{OFF}$$

$$\frac{N_{NC}^{HE\ MC}}{N_{NC}^{ON\ MC}} N_{NC} + \frac{N_{CC}^{HE\ MC}}{N_{CC}^{ON\ MC}} N_{CC} + \frac{N_{\nu_e}^{HE\ MC}}{N_{\nu_e}^{ON\ MC}} N_{\nu_e} = N_{data}^{HE}$$

Monte Carlo	
NC	(65±23)%
$\nu_\mu$ -CC	(24±8)%
$\nu_e$ -CC	(11±2)%

Data Driven	
NC	(64±5)%
$\nu_\mu$ -CC	(23±5)%
$\nu_e$ -CC	(13±3)%



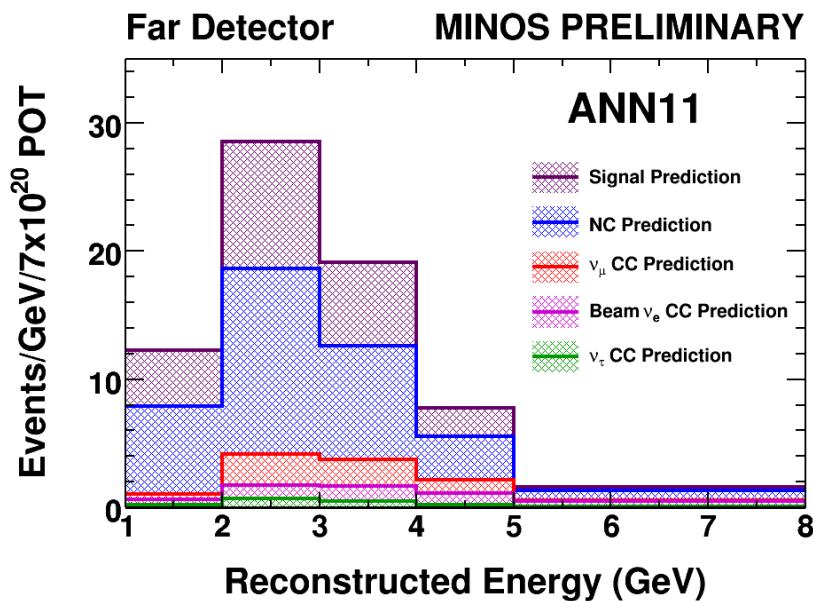
# F/N Extrapolation

- Use ND measurement of NC,  $\nu_\mu$  CC and beam  $\nu_e$  CC backgrounds to predict FD background:

**FD prediction for component  $\alpha$  in energy bin i**

$$F_i^{predicted,\alpha} = N_i^\alpha \times \left( \frac{f_i^\alpha}{n_i^\alpha} \right)_{\text{ND data}}$$

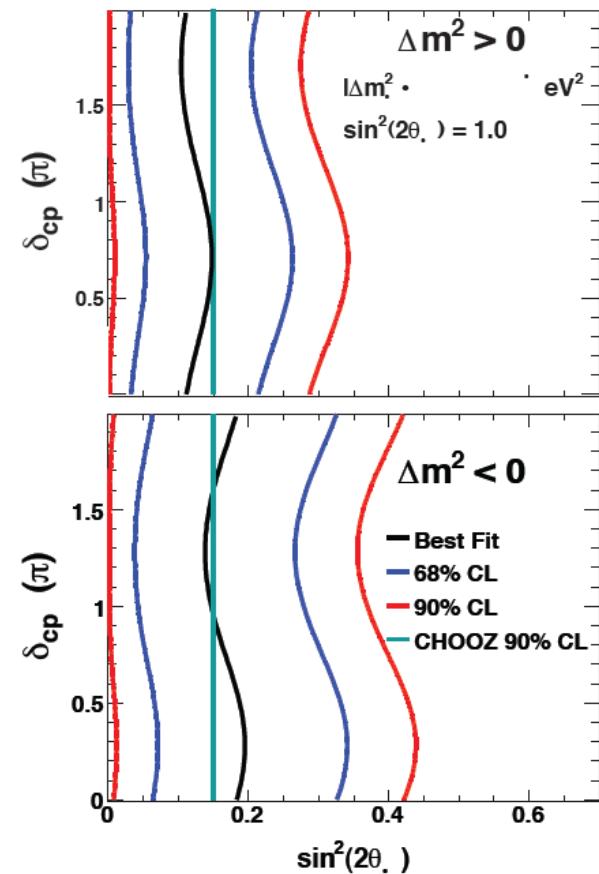
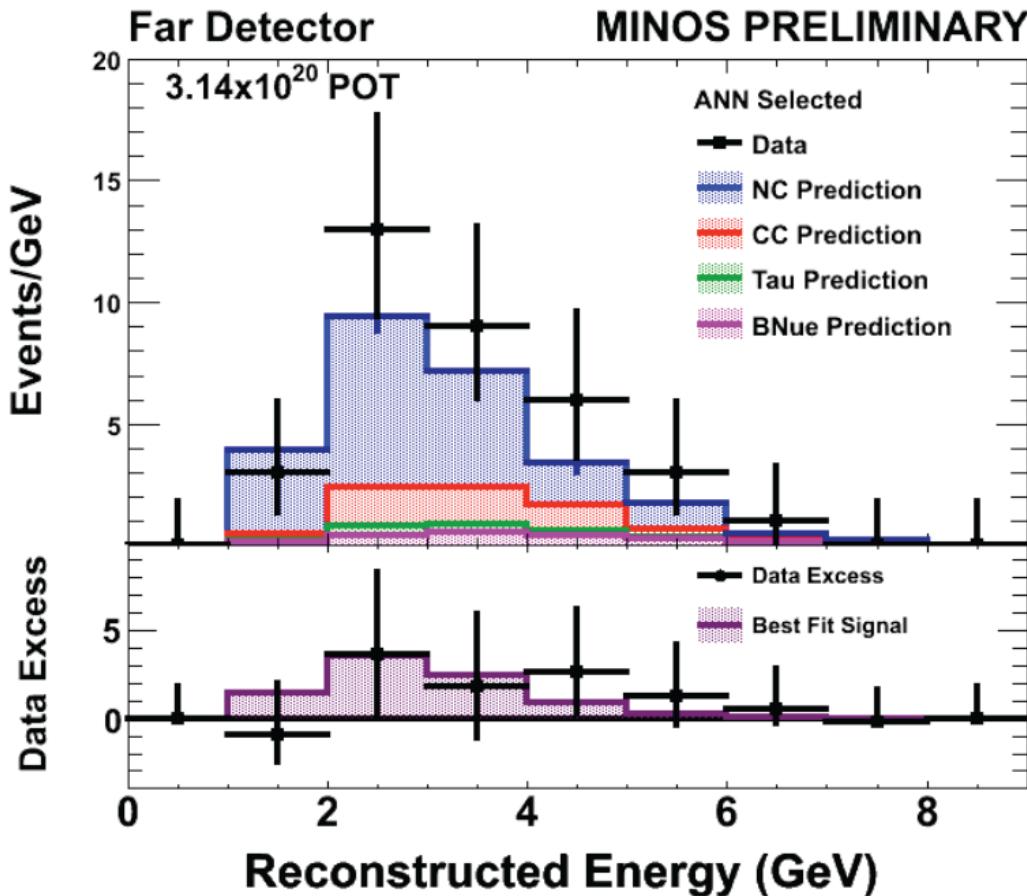
**F/N ratio of MC selected events from component  $\alpha$  in energy bin i**



Component	#Event
NC	35.8
$\nu_\mu$ CC	6.3
Beam $\nu_e$ CC	5.0
$\nu_\tau$ CC	2.0
Total	49.1
Background	
$\nu_e$ CC signal	23.9

$\sin^2(2\theta_{13})=0.15$  (CHOOZ limit),  $|\Delta m^2_{31}|=2.43\text{e-}3\text{eV}^2$ ,  $\sin^2(2\theta_{23})=1$ .

# $\nu_e$ $3 \times 10^{20}$ POT Results



- \* We observe 35 events, and expect  $27 \pm 5$  (stat)  $\pm 2$  (syst) events.
- \* Results are  $1.5 \sigma$  high:  $\sin^2(2\theta_{13})=0$  is included at the 92% level.

# $\nu_\mu$ CC Disappearance

- Precision measurements of atmospheric  $\Delta m^2$  and  $\sin^2(2\theta)$ .
- Test the neutrino oscillation hypothesis.

*Look for a deficit of  $\nu_\mu$  events in the Far Detector .*

$$P(\nu_\mu \rightarrow \nu_\mu) = 1 - \boxed{\sin^2 2\theta} \sin^2 \left( \frac{1.27 \boxed{\Delta m^2} L}{E} \right) \quad L=735 \text{ km}$$

